

# The Forcing of the Pacific Decadal Oscillation

**Niklas Schneider**

International Pacific Research Center and Department of Oceanography, University of  
Hawaii, Honolulu

**Bruce D. Cornuelle**

Scripps Institution of Oceanography, University of California, San Diego

Corresponding author:

N. Schneider, IPRC, University of Hawaii at Manoa, 1680 East West Road, Honolulu,  
HI 96822. Phone (808) 956-8383, fax (808) 956-9425, email: nschneid@hawaii.edu

**Abstract.** The Pacific Decadal Oscillation (PDO), defined as the leading empirical orthogonal function of North Pacific sea surface temperature anomalies (SSTA), is a widely used index for decadal variability. We show that the PDO can be recovered from a reconstruction of North Pacific sea surface temperature anomalies based on a first order, autoregressive model and forcing by variability of the Aleutian Low, by El Niño/Southern Oscillation (ENSO), and by oceanic zonal advection anomalies in the Kuroshio-Oyashio Extension. The latter results from oceanic Rossby waves forced by North Pacific Ekman pumping. The SST response patterns to these processes are not orthogonal, and determine the spatial characteristics of the PDO. The importance of the different forcing processes is frequency dependent. At interannual time scales, forcing from ENSO and the Aleutian Low determine the response in equal parts. At decadal time scales, zonal advection in the Kuroshio-Oyashio Extension, ENSO and anomalies of the Aleutian Low each account for similar amounts of the PDO variance. These results support the hypothesis that the PDO is not a dynamical mode but results from the superposition of sea surface temperature fluctuations with different dynamical origins.

## 1. Introduction

The Pacific Decadal Oscillation (PDO, Mantua et al. 1997) is a widely used index to characterize North Pacific decadal variability and anomalies of Northern Hemisphere climate and the North Pacific ecosystem. Yet, the processes underlying the temporal and spatial characteristics of the PDO have not been clarified. Here, we present a statistical analysis of North Pacific sea surface temperature, sea level pressure and wind stress to identify the drivers of the PDO and their relative contributions to its temporal and spatial patterns.

The PDO is defined as the leading empirical orthogonal function (EOF) of monthly anomalies (deviations from the climatological annual cycle) of sea surface temperature (SST) in the Pacific poleward of 20°N (Davis 1976, Mantua et al. 1997)<sup>1</sup>. Its temporal evolution (Fig. 1) is marked by variability on interannual and decadal time scales, with several pronounced shifts, the 1976/77 transition being the most famous and extensively studied (Trenberth 1990, Graham 1994, Trenberth and Hurrell 1994, Miller et al. 1994). The spatial pattern of the PDO (Fig. 2) resembles a horse-shoe with temperature anomalies in the central North Pacific surrounded by anomalies of opposite sign in the

---

<sup>1</sup>In the original definition of the PDO, the global monthly mean SST anomaly is removed prior to the calculation of the EOF. The leading EOF of this field and of the raw monthly SST anomalies are barely different, and we consider the raw SST anomalies. This is dictated by our desire to develop a regression model for the North Pacific SST anomalies, without attempting a similar model for the global mean of SST.

Alaska gyre, off California, and toward the tropics.

The PDO and its associated sea level pressure pattern have attracted considerable attention since their time evolutions are correlated with anomalies of the Pacific ecosystem (Mantua et al. 1997), with North American precipitation, stream flow and surface temperature anomalies (Mantua and Hare 2002, Dettinger et al. 1998, Cayan et al. 1998), with surface temperature anomalies in North–Eastern Asia (Minobe 2000), with fluctuations of the Asian Monsoon (Krishnan and Sugi 2003), and with a modulation of El Niño/Southern Oscillation (ENSO) teleconnections (Gershunov and Barnett 1998). This co-variation can result from the PDO forcing the atmosphere, or from a common forcing of the PDO and co-varying climate anomalies. Model experiments suggest the latter explanation for the decadal modulation of ENSO teleconnections (Pierce 2002). However, this question has not been clarified from observations, and requires the identification of the forcing mechanism of the PDO.

The PDO pattern is qualitatively consistent with atmospheric forcing associated with fluctuations of position and strength of the Aleutian Low. In the central North Pacific, a deepened Aleutian Low decreases SST by advection of cool and dry air from the north, by increases of westerly winds and ocean-to-atmosphere turbulent heat fluxes, and by strengthened equatorward advection of temperature by Ekman currents. In the eastern regions, a deepened Aleutian Low enhances poleward winds and leads to warm anomalies of surface temperature.

However, this qualitative picture hides the complex processes governing changes of the Aleutian Low and North Pacific SST anomalies. The North Pacific atmosphere

affects the surface heat budget via anomalies of surface fluxes and Ekman advection (Alexander et al. 1992), and via the excitation and propagation of Rossby waves that affect the upper ocean in the Kuroshio-Oyashio Extension region (Miller et al. 1998, Deser et al. 1999, Xie et al. 2000, Miller and Schneider 2000, Seager et al. 2001, Schneider et al. 2002, Qiu 2003). The anomalies of the atmosphere reflect its intrinsic variability (Davis 1976, Pierce et al. 2001, Barnett et al. 1999, An and Wang 2005), interannual variability associated with El Niño/Southern Oscillation (ENSO, Newman et al. 2003), that are teleconnected to the North Pacific (Alexander et al. 2002, Alexander et al. 2004), and remote forcing from other areas in the tropics (Deser et al. 2004) and possibly elsewhere. Tropical ENSO variability also influences North Pacific SST anomalies via poleward propagating coastal Kelvin waves along the Pacific coast of the Americas (Chelton and Davis 1982, Clarke and Lebedev 1999).

Here, we quantify the forcing mechanism of North Pacific SST and the PDO, and investigate the hypothesis that the PDO time evolution and spatial pattern result from a superposition of these different forcing mechanism. To this end we reconstruct North Pacific SST anomalies (SSTA) using a first-order, autoregressive (AR-1) model forced indices that track ENSO, sea level pressure variations of the Aleutian Low, and oceanic changes in the Kuroshio-Oyashio Extension. The leading EOF of this reconstruction is nearly identical to the observed PDO, and allows an investigation of its properties.

In the following, we introduce the data and forcing indices, and present the method, skill and interpretation of the SSTA reconstruction. This reconstruction is then used to determine and discuss the PDO kinematics, its evolution, including the relative

importance of tropical versus North Pacific forcing, its spectrum and predictability.

## 2. Data

Throughout this study, we use monthly anomalies from the average seasonal cycle of SST, sea level pressure, and wind stress from the NCEP/NCAR reanalysis of the period from 1950 to 2003 (Kalnay et al. 1996). The PDO used here is based on the leading EOF of July to June annual averages of SSTA, rather than on monthly anomalies (Mantua et al. 1997). The July to June annual average focuses on the winter season when both teleconnected forcing from the tropics and intrinsic atmospheric variability are most pronounced (Newman et al. 2003). Annual averages of the leading principal component based on monthly anomalies are basically identical with the PDO used here, with correlation coefficients of 0.994 (Fig. 1 top). To extend the study back in time, we also employ 1900 to 1997 time series of the observed PDO time index, the North Pacific Index of sea level pressure in the Aleutian Low ( $NPI_T$ , Trenberth and Hurrell 1994), the cold tongue index CTI of equatorial Pacific sea surface temperature anomalies, all available from [http://tao.atmos.washington.edu/data\\_sets](http://tao.atmos.washington.edu/data_sets), and the Optimal Tropical Index OTI (Deser et al. 2004), available from <http://www.cgd.ucar.edu/~cdeser/Data/>.

## 3. Forcing indices

North Pacific SST anomalies are associated with ENSO, with atmospheric variations intrinsic to the North Pacific, and, in the Kuroshio-Oyashio region, with oceanic Rossby waves excited by North Pacific Ekman pumping. The time evolution of each of these

processes will be represented by an index time series, to be identified in this section by a combination of physical reasoning and statistical optimization.

### 3.1. ENSO and North Pacific Index

The North Pacific SST is composed of at least two temporally independent anomaly patterns: one associated with ENSO, and one due to variations of atmospheric pressure intrinsic to the North Pacific (Davis 1976, Alexander 1992, Nakamura et al. 1997, Zhang et al. 1997, Nakamura and Yamagata 1999, Tomita et al. 2001, Barlow et al. 2001, Nakamura and Kazmin 2003, An and Wang 2005). The impact of ENSO, represented by the NINO3.4 temperature anomaly in the eastern equatorial Pacific (170°W to 120°W, 5°S to 5°N) has been documented by Newman et al. (2003), by assuming that annual averaged values of the PDO amplitude are governed by an AR-1 process, forced by the NINO3.4 time series. Correlations of North Pacific anomalies of sea level pressure and SST and of changes in the warm pool region and South Pacific convergence zone indicate that processes in these areas also impact the North Pacific (Deser et al. 2004, Garreaud and Battisti 1999). In addition, intrinsic variability in the extra-tropical atmospheric circulation, particularly, changes in the position and strength of the Aleutian Low (Trenberth and Hurrell 1994) and associated storm track activity, forces North Pacific SST anomalies (e.g. Pierce et al. 2001, Pierce 2001).

To identify forcing indices of the PDO, we search for regions where sea level pressure anomalies have skill in reconstructing the observed time series of the PDO amplitude. We extend the approach of Newman et al. (2003) and assume that the July

to June averages of the PDO amplitude  $D$  are governed by an AR-1 process, forced by the concurrent July to June averages of anomalies of sea level pressure ( $F_{SLP}$ )

$$D(t) = \alpha' D(t-1) + \gamma' F_{SLP}(t) \quad (1)$$

where  $t$  is time in years. The damping coefficients  $\alpha'$  and regression coefficients  $\gamma'$  are determined by a least square fit (see appendix A) of equation (1) to the observed values  $D$  and  $F_{SLP}$ , one location at a time. Using this fit, the entire history of the observed PDO amplitude  $D$  is reconstructed from the observed initial condition and SLP anomaly time series.

The correlation between observed and reconstructed PDO amplitude, plotted at the location of the forcing time series (Fig. 3, upper panel), shows high values in the North Pacific ( $>0.8$ ), and in the eastern South Pacific, West Pacific warm pool, the eastern Indian Ocean, and the tropical Atlantic, and indicates that SLP at these locations has skill in the reconstruction of the PDO. The tropical signals are associated with ENSO: Removing the regression with NINO3.4 from SLP anomaly time series, and repeating the fitting exercise removes all the centers of high PDO amplitude reconstruction skill in the tropics, with only the North Pacific center remaining, albeit with reduced correlation (Fig. 3, lower panel). This suggests that sea level pressure in the central North Pacific and tropical forcing as described by NINO3.4 account for the majority of the variations of the PDO time amplitude.

The average of sea level pressure in the area where reconstruction skill without NINO3.4 exceeds of 0.55 (dithered region in Fig. 3, lower panel) serves as an index for



the North Pacific atmospheric forcing, and will be referred to as North Pacific Index (NPI), since it is approximately co-located (and highly correlated, at 0.85) with the index by the same name introduced by Trenberth and Hurrell (1994), here called  $NPI_T$ . These indices describes anomalies of the Aleutian Low, the primary mode of variability of annual averaged anomalies of North Pacific sea level pressure: The leading EOF of July to June averages of surface pressure explains more than half of the sea level pressure variance, and has a correlation with the Trenberth and Hurrell index in excess of 0.9. In contrast to the primarily interannual variations of NINO3.4, the monthly values of the NPI show variability on all time scales (Fig. 1).

### 3.2. Ocean circulation anomalies in the Kuroshio-Oyashio Extension

In the boundary currents of the Northwestern Pacific, fluctuations of the wind driven circulation affect sea surface temperature (Xie et al. 2000). These circulation anomalies result from the accumulation of North Pacific Ekman pumping  $F_{Ek}$  along Rossby wave trajectories

$$\partial_t p - c \partial_x p = F_{Ek} \quad (2)$$

where  $p$  is the amplitude of a first baroclinic mode Rossby wave, and represents an index for the depth of the thermocline, and  $c$  is the Rossby wave speed (Sturges and Hong 1995, Schneider and Miller 2001). The anomalies of  $p$  affect the position and sharpness of the Kuroshio-Oyashio Extension and cause anomalies of surface temperatures, either directly through changes of thermocline depth and meridional shifts of the Kuroshio-Oyashio frontal system (Seager et al. 2001, Schneider et al. 2002),

or by anomalies of zonal advection (Qiu 2003). The former process is most effective in the winter season, when deep mixed layers couple thermocline depth and SST (Xie et al. 2000, Schneider et al. 2002), and is simulated by assuming that anomalies of SST and thermocline depth  $p$  are proportional. The latter process, anomalous zonal advection, invokes the meridional gradient of pressure, and is affected by the meridional dependence of the forcing and of the Rossby wave speed  $c$ . Anomalous advection acts year round, and should therefore be more important for annual averages.

To derive indices for the impact of this gyre adjustment on SST, anomalies of  $p$  are estimated from equation (2) for the North Pacific, with the Ekman pumping calculated from anomalies of the NCEP/NCAR reanalysis wind stress (Schneider and Miller 2001). The Rossby wave speeds are based on satellite observations of sea level (Qiu 2003). The estimates  $p$  are averaged in the Kuroshio-Oyashio Extension between 140°E and 170°E, and a thermocline depth index  $P_{AVG}$  is then obtained by the average between 35°N and 40°N; the zonal advection index  $P_{DEL}$  is evaluated by differencing the zonal averaged  $p$  between 38°N and 40°N. The latitudes correspond to the location of the Kuroshio-Oyashio Extension region and were refined by trial and error, a prospecting considered in the estimation of the significance (see below).

The Kuroshio-Oyashio Extension thermocline depth index  $P_{AVG}$  and zonal advection index  $P_{DEL}$  are dominated by variance at decadal frequencies (Fig. 1), as expected from the integration of atmospheric forcing along Rossby wave trajectories (Frankignoul et al. 1997), and can only to account for a significant fraction of SSTA at long time scales. The KOE indices are largely independent of wind stress curl anomalies

associated with NINO3.4 and NPI. Removal of the regression of the wind stress curl with these indices before solution of equation (2) has very little impact on  $P_{DEL}$  and merely removes a trend from  $P_{AVG}$  (dotted lines in Fig. 1).

## 4. Reconstruction of SST

The PDO is defined as the leading mode of SSTA, so we begin by reconstructing SSTA, and will later return to examine how well the leading EOF of the reconstructed SSTA compares to the actual PDO.

### 4.1. Approach

The budget for surface temperature anomalies  $T$  is assumed to be governed by an AR-1 model (Hasselmann 1976)

$$\partial_t T(x, y, t) = -\tilde{\alpha}(x, y)T(x, y, t) + \gamma_i(x, y)\tilde{F}_i(t) \quad (3)$$

where  $t$  is time,  $\tilde{\alpha}$  is the damping time scale, and the different forcing terms, denoted by index  $i$ , have the time evolution  $\tilde{F}_i$  with spatial footprint  $\gamma_i$ , and a repeated index  $i$  implies the Einstein summation convention. The first term on the right side represents the damping of SST anomalies by the air–sea heat fluxes, with a decay rate  $\tilde{\alpha}$  determined by the feedback of the air-sea heat flux and by the mixed layer depth. While these processes and thus  $\tilde{\alpha}$  have a seasonal cycle, we focus on time scales longer than a year, so that  $\tilde{\alpha}$  is taken as a constant, representative value for the entire year. Considering heat content from the surface to winter mixed-layer depths would remove the complications associated with the seasonal cycle of mixed layer and the re-emergence of temperature

anomalies (Deser et al. 2003). However, the PDO is defined with respect to SST, and we need to determine the relationship between seasonal variations due to re-emergence, and the representative, annual value  $\tilde{\alpha}$  of the feedback. In appendix B, an extension of the Hasselmann (1976) model to include re-emergence is used to show that  $\tilde{\alpha}$  derived from annual averages of SST lies between summer and winter damping rates, but close to winter values.

Equation (3) is discretized to describe the year to year evolution of July to June averages of temperature anomalies. With  $\tilde{\alpha}$  a constant in time, equation (3) is integrated over one year, and then averaged from July to the subsequent June. This yields for the annual averaged value of temperature anomalies at every location  $x$

$$\overline{T(x, y, t)} = \gamma_i(x, y) \overline{\int_{t-\delta}^t dt' \tilde{F}_i(t') e^{-\tilde{\alpha}(x, y)(t-t')}} + e^{-\tilde{\alpha}(x, y)\delta} \overline{T(x, y, t - \delta)} \quad (4)$$

$$=: \gamma_i(x, y) F_i(x, y, t) + \alpha(x, y) \overline{T(x, y, t - \delta)} \quad (5)$$

where  $\delta$  is the one year time step of the discretization, and the overline represents July to June 12 month averages. The annual average value of SSTA results from its value of the previous year, discounted at a rate of  $\tilde{\alpha}$ , and the annual averages of the forcing fields, which have been filtered by a one-sided exponential with decay  $\tilde{\alpha}$  due to the damping of temperature anomalies. For ease of reference,  $F_i$  is defined in equation (5) as the annual average of the filtered forcing time series with filter coefficients varying in  $x, y$ , and  $\alpha = \exp(-\tilde{\alpha}\delta)$  is the discretized autoregressive parameter.

The discretized temperature equation (4) preserves lead-lag relationships of equation (3) between the forcing and temperature, unlike the ad-hoc approach of

equation (1) that relates the value of the PDO to contemporaneous forcing fields. A slight complication arises from the spatial dependence of  $\tilde{\alpha}$  that renders the filtered forcing function  $F_i$  a function of time and space, and produces non-separable forcing for the evolution of annually averaged temperature anomalies. However, we will find that  $\tilde{\alpha}$  has only a weak spatial dependence so that the spatial variance of forcing functions  $F_i$  are small and not important.

The reconstruction of North Pacific SST anomalies thus reduces to an exercise of fitting the observed evolution of  $\overline{T(x, y, t)}$  to the right hand side of equation (4) by adjusting the damping  $\tilde{\alpha}(x, y)$  and spatial footprints of the forcing  $\gamma_i(x, y)$  at every location. Equation (4) is nonlinear in  $\tilde{\alpha}$  due to the filtering of the forcing time-series, and the coefficients are determined iteratively. Starting from a first guess of  $\tilde{\alpha}$ , the time integrals of  $\tilde{F}_i$  and June to July averages are formed to yield  $F_i$ . We then determine  $\alpha$  and  $\gamma_i$  from equation (5) by multi-linear regression using a least-squares approach (see Appendix A), and repeat the procedure with the new estimate of  $\tilde{\alpha}$  obtained from  $\alpha$ . Typically, this procedure converges in less than ten iterations.

The skill of the fit is determined by comparison of the observed and fitted temperatures, and is obtained in two related ways: as a one year “forecast” of year  $n$  from observed, previous year’s SSTA and the forcing time series<sup>2</sup> (the procedure followed by Newman et al. 2003 when comparing the observed and fitted time-evolution

---

<sup>2</sup>Note that this is not strictly a prediction since the values of the forcing time series are assumed to be known up to time  $n$

of the PDO), or from a 50 year “hindcast”, initializing equation (5) with the observed 1950/51 July to June average and determining the evolution until 2002/03 using only the forcing time series. The two approaches yield essentially the same results, albeit with the hindcast, the more demanding test, exhibiting overall lower skill values than the forecast, and we will present the hindcast skills only.

The significance of the reconstruction and of each regression pattern is estimated by comparison to the performance of the null hypothesis: that a selection of random red noise series can do as well as the physically meaningful series chosen here. Figure 4 shows the 95% highest correlation level from one thousand reconstructions of the annual averaged values of the PDO from red noise time series that have the same one year lag autocorrelation as the annual averages of the index series  $F_i$ . To account for artificial skill, we repeat the “prospecting” used in choosing the NPI,  $P_{AVG}$  and  $P_{DEL}$  with the noise time series by assuming that the NPI was selected out of North Pacific sea level pressure from 20 independent regions or modes, and that the  $P_{DEL}$  and  $P_{AVG}$  were selected each from a total of five possible latitude bands. These estimates of the degrees of freedom are deliberately high, so as to yield a conservative estimate of significance.

Specifically, each reconstruction of the PDO from noise time series is obtained just as in the analysis of the observations. The observed PDO is fit to an AR-1 process forced by one “NINO3.4” noise realization. The residual is then reconstructed using twenty independent “NPI” noise time series, and the realization with the best fit is chosen. We then choose the best of five noise realizations each for  $P_{DEL}$  and  $P_{AVG}$  that capture SSTA variations of a representative time series in the western North Pacific.

For this set of “best” noise forcings, we obtain the PDO reconstruction skill, and then determine at every point in the North Pacific the combined skill of the noise series in the reconstruction of observed SSTA and the individual skill of each of the forcing indices.

For the PDO reconstruction, this yields 95% (90%) significance levels of the hindcast correlation of 0.68 (0.66). The 95% significance levels of SSTA reconstruction skill (Fig. 4) reach values of 0.6 to 0.65 in the central and eastern North Pacific, and mimic the horse-shoe pattern of the PDO. The 95% significance levels of the individual forcing indices vary about 0.4 for NINO3.4, and between 0.45 to 0.55 for NPI,  $P_{DEL}$  and  $P_{AVG}$ .

#### 4.2. Skill

The reconstruction of SSTA based on the forcing indices of ENSO, NPI,  $P_{DEL}$  and  $P_{AVG}$  is very successful in the North Pacific. Correlations of the hindcast and observations of SSTA (Fig. 5) are larger than 0.75 in the areas of large loading of the PDO in the central and eastern North Pacific (Fig. 2, top) and mimic closely the variance of SSTA explained by the PDO itself. The skill in these regions is significant as it exceeds the 95% significance levels derived above (Fig. 4). Only in the areas south of 25°N, and along the zero line of the PDO pattern does the reconstruction not pass the significance test.

Central to our purpose here is the comparison of the leading EOF of SSTA and its reconstruction from the hindcast. The spatial patterns of original and reconstructed fields are basically identical (Fig. 2), with a pattern correlation in excess of 0.9 (Table

1). Small differences occur in the amplitudes of the spatial pattern in the central North Pacific, where the ridge of high loading extends further east in the reconstruction. The principal component shows a similar good fit. The correlation of observed and reconstructed PDO is 0.93, highly significant, (Fig. 6, Table 1), with all transitions being captured. The only differences occur in slightly reduced amplitudes in the late 1950s and 1990. This suggests that the processes underlying the PDO are captured, and the reconstruction can be used to explore the properties of the PDO.

The hindcast skill of the individual components (Fig. 5) shows that NINO3.4, NPI and  $P_{DEL}$  account for significant fractions of North Pacific SSTA variability. The skill of NINO3.4 is largest in the eastern portion of the basin and along the coast of North America, while NPI accounts for the largest variations along 40°N and in the central and the western portion of the Pacific. The zonal advection index has skill in the Kuroshio-Oyashio Extension, as expected. The contribution of  $P_{AVG}$ , while revealing a physically plausible pattern as will be discussed below, nowhere exceeds the skill expected from an arbitrary red noise process, and  $P_{AVG}$  will therefore not be considered in the reconstruction of the PDO.

### 4.3. Damping time-scale

The lag 1 autocorrelation of annual averages of SSTA,  $\alpha$ , is largely a constant in space with typical values of 0.2 to 0.3, and corresponds to a damping time scale  $\tilde{\alpha}^{-1}$  of 7.5 to 10 month (Fig. 7). Off the coasts of Japan and China the damping times are larger, but in these areas skill is small, and not significant (Figs. 4, 5). The damping



time reflects the feedback  $\epsilon$  to surface temperature of the air-sea heat flux, normalized by an effective mixed-layer depth  $H$ , and the density  $\rho_0$  and heat capacity  $c_p$  of sea water. With  $\epsilon = 15 \text{ W m}^{-2} \text{ K}^{-1}$  (Deser et al. 2003),  $\rho_0 = 1000 \text{ kg m}^{-3}$  and  $c_p = 4 \cdot 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ , the effective annually averaged, mixed-layer depth is  $H = \epsilon(\rho_0 c_p \tilde{\alpha})^{-1}$  varies between 74 m and 98 m. This is shallower than the deep winter-time mixed-layer depths required to explain the auto-correlation of upper-ocean heat content (Deser et al. 2003), but consistent with our focus on annually averaged sea surface temperature anomalies and typical mixed-layer depths of the North Pacific (see Appendix B).

#### 4.4. Forcing time series

Given the damping time-scales, the filtered forcing time series  $F_i$  can be obtained and are shown in Fig. 6 normalized to unit standard deviation. The filtered NINO3.4 series shows the major El Niño and La Niña events, slightly delayed as expected from the integration. The 1976/77 change is marked by several years of depressed NINO3.4, followed after the shift by a recovery to near normal forcing. The NPI time series displays more year to year variability, and also shows a trend to more negative values, punctuated by dramatic variations of either sign. The transition to higher values after 1986 corresponds to an intensified Pacific storm track reported by Nakamura et al. (2002, their Fig. 5).

The spatial dependence of each  $F_i$  is shown in Fig. 6 by its spatial average (thin black line), and its standard deviation (vertical bars). As expected from the small variability of  $\tilde{\alpha}$ , the scatter of  $F_i$  is small, so small in fact, that the standard deviation

is only perceptible for NPI, which has the largest variance at high frequencies, and is therefore most sensitive. The pressure indices are hardly changed from their unfiltered  $\tilde{F}_i$ , since their variance is dominated by interannual and decadal time scales, and not affected by the filtering operation. Thus, our calculations and the forcing footprints  $\gamma_i$  are insensitive to the exact values of  $\tilde{\alpha}$  in the filtering of the monthly forcing indices  $\tilde{F}_i$  to the annual averages  $F_i$ , and much the same results are obtained by filtering the forcing functions with a value of  $\tilde{\alpha}^{-1}$  of 3/4 year.

#### 4.5. Orthogonalization matrix

The forcing time series  $F_i$  are not independent, and we have to account for their shared variance. While the independent components of each  $F_i$  are sufficient to determine their unique regression patterns that affect SST directly, their correlated components imply that any particular forcing has an indirect impact through the other time series. To quantify these relationships we determine the rotation matrix  $B_{ij}$  that relates  $F_i$  to an orthogonal base  $F_j^*$

$$\gamma_i F_i(t) = \gamma_i B_{ij} F_j^*(t) \quad (6)$$

with rotated regression pattern  $\gamma_j^* = \gamma_i B_{ij}$ . The matrix  $B_{ij}$  is obtained from a Gram-Schmidt orthogonalization that leaves the NINO3.4 time series unchanged, removes from NPI the regression with NINO3.4, removes from  $P_{DEL}$  the the multi-linear regression with NINO3.4 and NPI, and so on. This order reflects the hypothesis that anomalies of Aleutian Low pressure, the NPI, result in part from teleconnections from

the tropics, i.e. NINO3.4, and that anomalies in the Kuroshio extension are in part a response to forcing of ENSO and of the NPI.

The rotation matrix  $B_{ij}$  (Table 2) is estimated with both  $F_i$  and  $F_j^*$  normalized to unit variance, so that the square of any element  $B_{ij}$  represents the variance of  $F_i$  captured by the  $F_j^*$ . Only two nontrivial relationships emerge: *NINO3.4* is negatively correlated with NPI and accounts for 30% of its variance, and  $P_{DEL}$  is weakly related to  $P_{AVG}$  and accounts for 6% of its variance – all the remaining elements are small. Thus, the rotated  $F_i^*$ , shown in Fig. 6 as dashed lines, only differ from  $F_i$  for NPI, and only slightly so for  $P_{AVG}$ .

Note that the Gram-Schmidt orthogonalization could start with NPI, and thus attribute the co-variance of NPI and *NINO3.4* to changes of the NPI. Physically, this suggests that the extra-tropics modulate ENSO via teleconnections to the tropics (Barnett et al. 1999b, Pierce et al. 2000) or provide stochastic forcing for ENSO (Vimont et al. 2001, Vimont et al. 2003). However, it seems unlikely that ENSO variability is completely determined by the NPI, and so we do not treat this option in detail although it is statistically appealing.

#### 4.6. Forcing footprints

The forcing terms  $\gamma_i(x, y)F_i(x, y, t)$  in equation (5) represent the annually averaged SSTA that is due to the forcing  $i$  after one year. Results are shown for  $F_i(x, y, t)$  normalized to unit standard deviation at every location, so that the maps of the regression coefficients  $\gamma_i(x, y)$  show the pattern of SSTA caused by a typical amplitude

of the filtered forcing time series  $F_i$ . Overall, the patterns are consistent with underlying physical processes and with results from prior studies.

The North Pacific Index NPI regression pattern dominates the regression (Fig. 8 bottom), with large amplitudes over the western North Pacific and the Kuroshio-Oyashio frontal regions, surrounded by anomalies of opposite sign in the eastern Pacific and in the Gulf of Alaska. A high sea level pressure perturbation of the Aleutian Low is associated with increased temperatures in the central North Pacific along  $40^\circ\text{N}$ , and cooler temperatures in the eastern Pacific, the Gulf of Alaska, and in the subpolar region (Davis 1976). These changes are associated with anomalies of the Pacific Storm track (Nakamura et al. 2002, An and Wang 2005), and are consistent with a decrease of westerlies that reduces turbulent heat losses and causes poleward Ekman advection in the central North Pacific. Cooling tendencies in the east are consistent with advection of cold and dry air from the high latitudes (Tanimoto et al. 2003).

The pattern associated with *NINO3.4* (Fig. 8 top) has most loading in the eastern Pacific and along the coast of North America, with opposite signed anomalies further offshore. This pattern captures coastal wave processes, and atmospheric teleconnections independent of the NPI, and, as we will show below, together with the correlated contribution of the NPI, forms the well known SST response pattern to tropical variations.

The zonal advection index in the Northwestern Pacific ( $P_{DEL}$ ) is associated with temperature anomalies in the Kuroshio-Oyashio Extension (Fig. 9 top) and overlaps with the regions of influence of the *NINO3.4* and NPI. A positive index, corresponding

to an increase of eastward flow, leads to warming centered west of the date-line and spreading along  $40^\circ\text{N}$ . The warming is shifted to the east-north-east of the region of the ocean-pressure index (indicated by dotted lines in Fig. 9), consistent with downstream advection by the mean flow, which has a east-north-easterly direction in the Kuroshio-Oyashio Extension (Qiu 2003).

The thermocline depth index ( $P_{AVG}$ ) in the Kuroshio-Oyashio Extension shows little effect on annual averaged SSTA (Fig. 9 bottom). Yet, the dipole pattern of warm anomalies at  $42^\circ\text{N}$  and cool anomalies at  $35^\circ\text{N}$  in response to a positive anomaly of  $P_{AVG}$  is consistent with a northward shift of the Kuroshio-Oyashio Extension axis. The weak signal is consistent with the annual cycle of mixed layer depth, which links thermocline depth and surface temperature only during the winter time when mixed-layers are deep (Schneider and Miller 2001). For annual averages, this process accounts for only a small fraction of the variance.

#### 4.7. Rotated forcing footprints

Now, let us look at the rotated forcing footprints. According to equation (6), the rotated forcing footprint  $\gamma^*$  of NINO3.4\* augments the unrotated ENSO footprint with the unrotated pattern of NPI,  $P_{DEL}$  and  $P_{AVG}$ , with weights  $B_{ij}$  given by the the first column of Table 2. The resulting NINO3.4\* pattern (Fig. 10 top) thus extends the unrotated NINO3.4 pattern (Fig. 8, top) to the west by, primarily, the addition of the unrotated NPI patterns (8, bottom). It is the canonical response of North Pacific SST to ENSO and corresponds to the composite ENSO response of the North Pacific, to the

ensemble averaged response obtained from models, and to the pattern removed from North Pacific SSTA by regression with an index for the cold tongue SSTA (Zhang et al. 1997).

The rotated  $\gamma^*$  of NINO3.4\* captures the annually averaged footprint due to the atmospheric bridge (Alexander et al. 2002, 2004) between ENSO (NINO3.4) and the Aleutian Low (NPI) and the atmosphere of the eastern North Pacific, and due to the oceanic connection by coastal wave propagation off North America equatorward of 40°N (Chelton and Davis 1982, Clarke and Lebedev 1999, Lluch-Cota et al. 2001). Overall, El Niño is associated with low temperatures in the central North Pacific in boreal fall and winter, and along the Kuroshio-Oyashio Extension in boreal summer (Alexander et al. 2004), and warm anomalies in the eastern Pacific and in the Gulf of Alaska. Alexander et al. (2002) attribute the anomalies of SST to changes of the surface heat flux, entrainment cooling and Ekman advection, together of the order of 20 W m<sup>-2</sup> in the cooling region east of the date line. Similar numbers are obtained from ship observations (Tanimoto et al. 2003). To compare this heat flux with the magnitude of the regression pattern of 0.2-0.3 K, we interpret the  $\tilde{F}$  time series of NINO3.4 (Fig. 1) as a heat flux time series, with anomalies during ENSO of 20 W m<sup>-2</sup> that are typical during ENSO events and equivalent to the 2 standard deviations. Applying this heat flux to a layer of 80 m depth, and estimating the corresponding  $F$  time series via the definition implied by equation (5) yields a standard deviation of annual averaged values of SSTA of 0.4 K, roughly consistent with Fig. 10 (top).

The rotated NPI\* pattern is almost identical to its unrotated counterpart, since

the contributions from  $P_{DEL}$  and  $P_{AVG}$  are small (second column of Table 2). The  $\gamma^*$  associated with  $NPI^*$  indicates that anomalies at  $40^\circ\text{N}$  (Fig. 10 bottom) are consistent with decadal, winter-time temperature anomalies independent of ENSO due to shifts of the North Pacific Subarctic fronts (Nakamura et al. 1997, Nakamura and Yamagata 1999, Nakamura and Kazmin 2003). The rotated pattern of  $P_{DEL}$  (not shown) is enhanced slightly between  $40^\circ\text{N}$  and  $45^\circ\text{N}$  west of the date line due to the contribution from  $P_{AVG}$  (Table 2, third column). Applying instead the variance shared between the two KOE indices to  $P_{AVG}$  enhances its northern loading. However, this increase is not sufficient to raise the variance associated with  $P_{AVG}$  beyond the significance level.

## 5. PDO properties

### 5.1. Kinematics

Using the auto-regressive model for SSTA and the regression patterns, we now investigate the evolution equation for the PDO. The equation governing the time evolution of the PDO is derived by projecting equation (5) on the leading empirical orthogonal function of annual averaged values of temperature anomalies

$$a_0(t) = \langle \alpha \Phi_0 \Phi_k \rangle a_k(t-1) + \langle \gamma_i \Phi_0 F_i \rangle \quad (7)$$

where  $a_k$  are the principal component and  $\Phi_k$  the orthonormal spatial loading pattern of mode  $k$ , with the PDO being  $k = 0$ , and  $\langle \dots \rangle$  denoting the spatial projection. In general, the spatial dependence of  $\alpha$  couples the evolution of the PDO and the other principal components. The forcing of the PDO amplitude, the last term on

the right hand side of equation (7) can be written for each  $i$  as the product of the regression coefficient  $\langle \gamma_i \Phi_0 \rangle$  and the weighted spatial average of the forcing time series  $\langle \gamma_i \Phi_0 \rangle^{-1} \langle \gamma_i \Phi_0 F_i \rangle$ . Since the spatial dependence of  $F_i$  is weak, the weighting has little effect, and the forcing time series for the PDO are indistinguishable from the spatial means of  $F_i(x, y, t)$  (compare black and gray lines in Fig. 6).

Using the estimates of  $\alpha$  and  $\gamma_i$ , and the observed  $\Phi_0$ , coefficients of equation (7) are estimated and presented in Table 3. The coupling of the PDO to higher modes is weak, and an autoregressive model for the PDO is appropriate, as assumed by Newman et al. (2003) and in equation (1). The damping coefficient for the PDO is 0.26, corresponding to a damping time of 8.9 months. This coefficient is about half the size of that obtained by Newman et al. (2003). In their analysis, the autocorrelation is determined after the regression with NINO3.4 is removed from the PDO time series. Thus, their residual includes the effect of the low frequency forcing by the ocean adjustment, and therefore overestimates  $\alpha$ .

The weights of the forcing fields projected onto the PDO are determined with  $F_i$  normalized to unit standard deviation, and shown as gray lines in Fig. 6. The forcing functions are indistinguishable from the individual  $F_i$  and their spatial means, showing the weak variations imparted by the spatial dependence of  $\tilde{\alpha}$ . While the forcing by NPI clearly dominates, a significant fraction of the NPI response results from teleconnections with NINO3.4. The orthogonalization to NINO3.4\* and NPI\* yields about equal weights for these forcings, with opposite signs. Thus ENSO primarily affects the PDO via changes of the Aleutian Low (and NPI), and leads to the known relationships between



ENSO and the PDO: warm conditions in the eastern equatorial Pacific are associated with a cool central North Pacific and a warm eastern North Pacific. Positive values of the NPI\* indicate a reduced Aleutian Low, with warmer temperatures in the central North Pacific (and thus negative anomalies of the PDO). The zonal advection index  $P_{DEL}$  in the Kuroshio-Oyashio Extension has about one third of the weight compared to the NPI\*, and indicates that increased advection leads to warm conditions and negative values of the PDO.

As a consistency test, we fit the observed evolution of the PDO amplitude to equation (7) while neglecting the coupling to higher EOFs of SSTA. This yields a slightly reduced damping coefficient, and very similar coefficients of the forcings (Table 3, bottom two rows).

In the following, we will restrict the discussion to the rotated forcing fields and regression pattern, noting that a significant fraction of the ENSO forcing affects North Pacific SSTA and the PDO via the NPI.

## 5.2. PDO evolution

The evolution of the PDO results from the sum of the temporal accumulation of the forcing by NINO3.4, changes of the Aleutian Low, and of the Kuroshio-Oyashio Extension, and their relative contributions can be estimated (Fig. 11). The shift in 1976/77 resulted primarily from NINO3.4\*, i.e. changes in the tropics (Trenberth 1990), with a small addition from changes of the NPI\*. In contrast, the shift from positive to negative conditions in 1998 was due to the NPI\*, with a smaller contribution from

NINO3.4\*.

Overall, the reconstruction recovers about 83% of the PDO variance. The identification of the variance accounted for by individual time series is complicated by the fact that, even though the forcing time series are orthogonal, their integrated contributions to the PDO are not. Thus, we estimate the variance explained by a particular index by the difference of the PDO variance obtained with and without this index. This shows that the unrotated NINO3.4 and NPI account for 21% and 73%, respectively, while the rotated NINO3.4\* and NPI\* account for approximately equal fraction of the PDO variance, 40% and 44%, respectively. The contributions of the zonal flow index  $P_{DEL}$  and  $P_{DEL}^*$  are much smaller, and corresponds to 6% and 7%, respectively of the year-to year PDO variance. Thus, the PDO is to a large part a reflection of the NPI, with NINO3.4 affecting the PDO both through the NPI and directly.

### 5.3. PDO spectrum

The frequency dependence of the forcing processes is best seen by a reconstruction of the frequency spectrum of the PDO (Fig. 12). To this end, results are applied to the monthly time series, and the spectral power  $P^2$  of the PDO is estimated as

$$P_{PDO}^2 = \frac{1}{\omega^2 + \tilde{\alpha}_0^2} (\gamma_i P_i)^2 \quad (8)$$

where  $\omega$  is the frequency,  $\tilde{\alpha}_0 = -\delta^{-1} \log_e(\langle \alpha \Phi_0 \Phi_0 \rangle)$ , and  $P_i^2$  are the power spectra of the forcing indices. The spectrum of the reconstruction has a very good agreement with

the observed spectrum (Fig. 12), with a slight overestimation at interannual frequencies, that can also be gleaned from the comparison of the reconstructed and observed PDO time series (Fig. 11). At annual and shorter time scales, the reconstructed spectrum slightly, but systematically underestimates the observed spectrum. This is consistent with re-emergence, observed in the PDO time series (Newman et al. 2003), and its impact on the spectrum (Appendix B).

The contribution  $(\omega^2 + \alpha_0^2)^{-1} \gamma_i^2 P_i^2$  of each of the forcing components  $i$  shows that the NPI\* contribution dominates the response at annual and higher frequencies, since the spectrum of the NPI\* itself is primarily white, with only a slight reddening tendency expected from thermodynamic air-sea coupling (Barsugli and Battisti 1998, Blade 1997), and a broad, gentle peak at interannual time scales, likely due to teleconnections to the tropics. The spectrum of NINO3.4\* has most power at interannual frequencies, with a strong low frequency component. Its contribution to the PDO increases rapidly, approximately as  $\omega^{-4}$ , toward interannual frequencies, and then decreases slightly toward decadal time scales. The spectrum of the zonal advection index  $P_{DEL}^*$  is red with all of its power at lower than interannual frequencies, and  $P_{DEL}^*$  adds to the power of the PDO only at decadal time scales. There, however, its contribution to the PDO is on par with the NPI\* and NINO3.4\*. Thus, the frequency spectrum of the PDO (Fig. 12) reflects the effects of the NPI\* at periods of a year and higher; at interannual frequencies, NINO3.4\* and NPI\* explain the variability, while at lower frequencies NPI\*, NINO3.4\* and  $P_{DEL}^*$  are of equal importance.

#### 5.4. Relation of PDO and regression patterns

Since the evolution of SSTA over the North Pacific is determined by three different forcing indices and patterns, so is the PDO. The regression patterns have large overlap, and are not orthogonal, and an empirical orthogonal function expansion can not separate these into distinct modes. In fact, we hypothesize that the PDO and the relative roles of its individual forcings are determined primarily by the spatial covariance of the forcing footprints, even if the time evolution of the forcing indices are independent.

To test this hypothesis, we note that the solution to equation (4) is separable if  $\alpha$  is a constant. This approximation is consistent with the lack of coupling of the PDO with higher modes. A reconstruction of SSTA for  $\alpha$  replaced at all locations with  $\alpha_0 = \langle \alpha \Phi_0 \Phi_0 \rangle$  results in almost identical estimates of the PDO (Fig. 2), with a pattern correlation of 0.98 and a temporal correlation of 0.93 with the observed PDO (Table 1).

The solution for annual averaged temperature anomaly at every location and time step  $t = n\delta$ , is obtained by integration of equation (5),

$$\bar{T}(x, y, t = n\delta) = \gamma_i^*(x, y) \sum_{j=1}^n \alpha_0^{n-j} F_i^*(t = j\delta) =: \gamma_i^*(x, y) f_i^*(t = n\delta) \quad (9)$$

and is the sum of separable products of the forcing footprints  $\gamma_i$  and the time integrals  $f_i$  of the AR-1 solution to each forcing index. The initial values  $f_i$  are obtained from a multi-linear fit of SSTA to the  $\gamma_i$  patterns at the initial time  $n = 0$ .

The covariance matrix  $\mathbf{R}$  of temperature anomalies, whose leading eigenvector is

the PDO, is then

$$\mathbf{R} = \overline{\mathbf{T}} \overline{\mathbf{T}}' = \boldsymbol{\gamma}^* \mathbf{f}' \mathbf{f}^* \boldsymbol{\gamma}^{*'} \quad (10)$$

where  $\overline{\mathbf{T}}$ ,  $\boldsymbol{\gamma}^*$  and  $\mathbf{f}^*$  are written in matrix notation, with prime denoting the transpose. The matrix  $\mathbf{R}$  is constructed from the covariance of the regression fields  $\boldsymbol{\gamma}^*$ , weighted by the covariance (correlation) of  $\mathbf{f}$ . The latter is dominated by the diagonal elements. To test whether the spatial pattern of the PDO is determined by the covariance of  $\boldsymbol{\gamma}$  even if the forcing indices are independent, a test covariance matrix  $\tilde{\mathbf{R}}$  is made using equation (10) by setting off-diagonal elements of  $\mathbf{f}'\mathbf{f}$  to zero. Again, the PDO pattern from this test matrix is almost identical to the observed pattern, with spatial and temporal correlations with observations of 0.98 and 0.93 respectively (Table 1), suggesting that the pattern of the PDO and the weights of the separate forcings result from the non-orthogonality of the forcing footprints. In fact, the pattern of the PDO can be recovered by considering only NINO3.4\* and NPI\* in the estimation of  $\mathbf{R}$  (Table 1, rightmost column) with a reduction of the skill of the principal component reconstruction commensurate with the lack of the contribution of  $P_{DEL}$ .

### 5.5. Robustness of PDO reconstruction

Deser et al. (2004) report that the relationship between winter values of Trenberth and Hurrell's (1994)  $\text{NPI}_T$  and NINO3.4, or the Cold Tongue Index (CTI, defined as SSTA in 180° to 90°W, 6°S to 6°N, with the global mean SSTA subtracted) was weaker in the first half of the 20th century than in the second half. However, the Optimal Tropical Index (OTI) – the leading EOF of a number of indices for western Pacific and

eastern Indian Ocean SSTA, anomalies of cloudiness and rainfall close to the South Pacific Convergence Zone, anomalies of stratus clouds in the eastern tropical Pacific, sea level pressure in the tropical Pacific and Indian Oceans – shows consistent variations with the NPI throughout the 20th century.

For the PDO, the question arises if its reconstruction is sensitive to the choice of tropical index, and if the relationship between PDO and its forcing is robust in the earlier part of the 20th century. To this end, 1900 to 1997 time series of the observed PDO,  $NPI_T$  and CTI or OTI are fitted to equation (4). Indices for the KOE can not be extended into the earlier half of the century since the wind stress estimates are not available, and forcing of equation (2) by a reconstruction of the Pacific wind stress from regressions with NINO3.4 and NPI fails to recover the KOE indices (see section 3.2).

The relationship of the PDO to the tropical indices alone is sensitive to the choice of the latter. Fitting the observed evolution of the PDO to the CTI only (Newman et al. 2003) leads a hindcast correlation of 0.52, while the fit of PDO to OTI captures more of the variance with a hindcast correlation of 0.65. However, when equation (4) is forced by  $NPI_T$  and either CTI or OTI, the hindcast skills for the time period 1900 to 1997 are 0.74 and 0.68, respectively. Thus, the variance of the  $NPI_T$  that can be attributed to tropical forcing is sensitive to the tropical index, but the tropical indices do not add any information to the reconstruction of the PDO, once the  $NPI_T$  (or NPI) is provided. The evolution of the PDO is largely determined by the NPI (Davis 1976), while the changes of the NPI are attributed in part to teleconnections from the tropics (Deser et al. 2004). However, please note that this does not imply that changes of the

Aleutian Low physically account for all changes of the PDO. Rather, prescription of the NPI index captures part of the tropical to extratropical teleconnections through the correlation of NPI and tropical indices.

The skill of the fit is degraded in the earlier part of the 20th century compared to the latter, with correlations for the period before (after) 1950 being 0.67 (0.85) for CTI and 0.61 (0.88) for OTI. Some degradation is expected since all indices are constrained by the fewer observations in the earlier period.

## 5.6. PDO predictability

Using the framework presented above, a forecast of the PDO requires predictions of NPI, ENSO and the gyre processes in the Kuroshio-Oyashio Extension. ENSO forecasts have skill at lead times of one and possibly up to two years (Barnston et al. 1999, Chen et al. 2004). The ENSO forecasts fix part of the NPI, the component of NPI\* due to intrinsic atmospheric variability of the Aleutian Low is expected to have very limited predictability, likely less than a year. The predictability of remote forcing from other areas, such as perturbations in the western Pacific or eastern Indian Ocean (Deser et al. 2004) remains to be determined. In the Kuroshio-Oyashio Extension, predictive skill with a lead time of one to two years has been documented for winter-time SSTA by virtue of the Rossby wave propagation (Schneider and Miller 2001). The predictability of  $P_{DEL}$  itself should be better, however, it only accounts for a small fraction of the year to year variability of the PDO. Thus, it appears that a forecast of annually averaged values of the PDO is possible at a lead time of up to a few years. This analysis does

not indicate much hope for a skillful forecast of the PDO at multi-year to decadal time scales.

## 6. Conclusion

Causes of decadal variability of SSTA in the North Pacific, and its leading empirical orthogonal function, have long been the subject of intense debate. Here, we show that the winter centered, annually averaged values of SSTA and the PDO can be reconstructed with high fidelity from an auto-regressive model forced by indices that track sea level pressure of the Aleutian Low, ENSO and ocean circulation anomalies in the Kuroshio-Oyashio Extension region. This implies that North Pacific SSTA and the PDO are a response to changes of the North Pacific atmosphere due to its intrinsic variability, due to remote forcing by ENSO and other processes, and due to ocean wave processes associate with ENSO and the adjustment of the North Pacific ocean by Rossby waves. The relative importance of these forcing processes for the PDO is frequency dependent: at periods shorter than a year, intrinsic North Pacific variability dominates; at interannual frequencies, changes of the Aleutian Low and of ENSO are essential; and at decadal periods, the ocean circulation anomalies in the Kuroshio-Oyashio Extension gain in importance to par with the other processes.

Under this hypothesis, the PDO is not governed by a single physical process that defines a climate mode, akin to ENSO, but results from at least three different processes. Of course, correlation is not causality, and statistical relations like this one can only be disproved, not proved, but we have presented physical arguments for the



hypothesized influences and have shown that randomly chosen red-noise processes do not approach the skill of the three indices used here. This hypothesis also exemplifies the well known limitation of empirical orthogonal functions that represent the variance optimally, but are not designed to separate multiple forcing fields with non-orthogonal spatial characteristics, as in the case of the PDO.

These results suggest a model for the origin of the PDO and quantify that both tropical and North Pacific processes are at play. The famous 1976/77 shift of the PDO is of tropical origin, as suggested in many previous studies (e.g. Nitta and Yamada 1989, Trenberth and Hurrell 1994, Graham 1994). The symmetry of SSTA pattern between the Northern and Southern extratropics is a reflection of the common tropical forcing (Evans et al. 2001).

This study further clarifies the causes of the “impact” of the PDO on climate of the adjacent continental areas and teleconnection patterns from the tropics. As found from modeling experiments by Pierce (2002), the PDO does not excite the climate modulation, but the PDO and these climate anomalies share the same forcing from the tropics and from intrinsic variability of the Aleutian Low. The impact of oceanic anomalies in the Kuroshio-Oyashio Extension complicates this picture at decadal time scales. The atmospheric response to these anomalies is likely small at best, and we do not expect a large trace of these in the climate over North America (Kushnir et al. 2002, Yulaeva et al. 2000). Furthermore, the relative roles of forcing are likely to be site dependent, and our results suggest therefore that the stratification of climate anomalies or teleconnection patterns be based on the underlying indices of ENSO and the NPI,

rather than ENSO and the PDO.

A similar conclusion applies to attempts to reconstruct Northern Hemisphere climate from paleo-data such as tree-rings (Biondi et al. 2001, Gedalof et al. 2002). The atmospheric conditions controlling tree growth and tree ring properties are a function of the tropical Pacific and the NPI, rather than of the PDO. Thus conditions in the tropical Pacific and the NPI can be reconstructed from an array of tree rings. A reconstruction of the PDO alone will likely miss the impact of ocean circulation anomalies in the Kuroshio-Oyashio Extensions, and has to be viewed with caution for decadal time scales that correspond to the adjustment time of the extratropical ocean circulation.

**Acknowledgments.** The authors thank Drs. Arthur J. Miller, Jim Potemra, Bo Qiu and Shang-Ping Xie for helpful discussions, and Clara Deser, Nathan Mantua, Hisashi Nakamura and one anonymous reviewer for comments on an earlier draft. This research was supported by the National Science Foundation, Grant OCE00-82543, by the Office of Science (BER), U.S. Department of Energy, Grants DE-FG03-01ER63255 and DE-FG02-04ER63862, and by the National Oceanic and Atmospheric Administration, Grant NA17RJ1231. The views expressed herein are those of the authors and do not necessarily reflect the views of NSF, DOE, or NOAA, or any of their sub-agencies. This is IPRC contribution # 335 and SOEST contribution # 6594.

## Appendix A: Least square solution

To find the coefficients of equations (1) and (5) at a point, we rewrite the problem in terms of the unknown parameters  $\mathbf{z} = (\alpha, \gamma_1, \gamma_2, \dots)$  and the matrix  $A$  with columns that are

the time series of each index, of the temperature or PDO amplitude average of year  $t - \delta$ , and of the forcing time series. The vector  $\mathbf{d}$  is the time series of observed temperature or PDO amplitude at year  $t$ , and the residual is  $\mathbf{r}$

$$\mathbf{d} = A \cdot \mathbf{z} + \mathbf{r} \quad (\text{A1})$$

The coefficients  $\mathbf{z}$  are determined by minimizing the cost function  $J$

$$J = \|\mathbf{d} - A \cdot \mathbf{z}\|_2 + \|\mathbf{z}\|_2 \quad (\text{A2})$$

The norms  $\|\cdots\|_2$  are chosen as the inverse covariance matrices

$$J = \mathbf{r}^T \cdot R^{-1} \cdot \mathbf{r} + (\mathbf{z})^T \cdot P^{-1} \cdot (\mathbf{z}) \quad (\text{A3})$$

where  $R$  is the covariance of the uncertainty in the residuals  $\mathbf{r}$ , and  $P$  is the covariance of the model parameters  $\mathbf{z}$ .

$J$  is minimized at the point  $\hat{\mathbf{z}}$ :

$$\min(J) = (\mathbf{z} - \hat{\mathbf{z}})^T \cdot \hat{P}^{-1} \cdot (\mathbf{z} - \hat{\mathbf{z}}) + \text{constant} \quad (\text{A4})$$

(Liebelt 1967). The inverse of the curvature at the minimum is  $\hat{P}$ , and it determines the uncertainty of the solution: how much the solution could vary while still doing a good job on the objective function.

The solution and uncertainty for the overdetermined system of the application here is obtained by inversion in model space

$$\hat{\mathbf{z}} = (A^T \cdot R^{-1} \cdot A + P^{-1})^{-1} \cdot A^T \cdot R^{-1} \cdot \mathbf{d} \quad (\text{A5})$$

with uncertainty covariance

$$\hat{P} = (A^T \cdot R^{-1} \cdot A + P^{-1})^{-1} \quad (\text{A6})$$

In this study, we employ a large signal-to-noise ratio, i.e.  $P^{-1} = 0$  and  $R = I$ , so that the cost function involves the misfit (residual) variance only. This implies that the parameter variance far exceeds that of the residuals, and that the elements of  $z$ , or the columns of  $A$ , have equal weight. Our solutions are insensitive to any large, but finite choice of signal-to-noise ratio.

## Appendix B: The impact of re-emergence

The focus on annual averages suppresses seasonal processes. The evolution of SST is particularly affected by the seasonal cycle of mixed layer depth. Temperature anomalies formed in deep winter and spring mixed layers persist under the seasonal thermocline during summer being insulated from the influence of the air-sea fluxes. During the erosion of the seasonal thermocline in the subsequent cold season, the deep anomalies are entrained into the mixed layers, and re-emerge at the surface. This re-emergence is found in the extra-tropical SSTA (e.g. Deser et al. 2003) and in the PDO time series (Newman et al. 2003), and represents an important departure from the AR-1 hypothesis for SST anomalies. Surface temperature anomalies not only depend on the anomalies of the prior month, but also on the anomalies of the previous cold season. This influences the power of SSTA at biannual to shorter than annual time scales (Dommenget and Latif 2002).

To investigate the impact of reemergence on our analysis of winter-centered, annual averages of SST, we explore a simple extension of the Hasselmann (1976) model that includes re-emergence. Consider a mixed layer with depth  $H_1$  in winter and  $H_2$  in summer months, with a summer seasonal thermocline in the layer between  $H_1$  and  $H_2$  ( $H_1 > H_2$ ). The rate of

change of the surface temperature  $T$  is governed by

$$\partial_t T = \frac{Q - \epsilon T}{\rho_0 c_p H} + \frac{H_2 - H_1}{\delta t} \frac{T - T_{st}}{H_2} \Lambda(t_{fall} \leq t \leq t_{fall} + \delta t) \quad (\text{B1})$$

with  $H = H_1$  from fall to spring, and  $H = H_2$  from spring to fall equinox. The air sea heat flux consists of a forcing term  $Q$ , and feedback component of strength  $\epsilon$ , normalized by the density of water  $\rho_0$  and its heat capacity  $c_p$ . The last term on the right hand side describes the erosion of the seasonal thermocline and is non-zero only during the entrainment season which commences at fall equinox  $t_{fall}$  and deepens the mixed layer to winter values during the period  $\delta t$ . This switch is indicated by the function  $\Lambda$  that is one only if its argument is true. The temperature of the seasonal thermocline  $T_{st}$  equals the surface values from the end of the fall entrainment period to spring equinox when the seasonal thermocline is non-existent and absorbed in the deep winter mixed layer. At the spring equinox at  $t_{spring}$  the mixed layer abruptly shallows to its summer depth, and the seasonal thermocline becomes insulated from the surface fluxes. Thus  $T_{st}$  remains at its spring value throughout the summer until the seasonal thermocline is re-entrained into the mixed layer in fall.

This model was implemented with parameters typical for the North Pacific  $\epsilon = 15 \text{ W m}^2 \text{ K}^{-1}$ ,  $\rho_0 = 1000 \text{ kg m}^{-3}$ ,  $c_p = 4000 \text{ J kg}^{-1} \text{ K}^{-1}$ ,  $H_1 = 100 \text{ m}$ ,  $t_{fall} = 0 \text{ months}$ ,  $t_{spring} = 6 \text{ months}$  and  $Q$  being Gaussian white noise  $Q$  with a standard deviation of  $20 \text{ W m}^{-2}$ . As the simplest case, we focus on a short entrainment season, and choose  $\delta t$  zero: In fall, the mixed layer instantly deepens to its winter depth. This idealized case recovers the qualitative influence of re-emergence. More gradual spring shallowing and fall entrainment seasons would simply smooth the autocorrelation function shown below. The model was run for 1024 years for the same realization of the random  $Q$  forcing for a reference case,  $H_2 = H_1$  identical to the Hasselmann (1976) model, and for summer time mixed layer depths of  $H_2 = 40 \text{ m}$  and of

$$H_2 = 20m.$$

The autocorrelation function of simulated  $T$  poses the characteristic structure of reemergence. While for the reference case the autocorrelation is independent of calendar month, shallow summer mixed layers result in an the autocorrelation for winter months that have secondary peaks in subsequent winters (Fig. B1). These secondary peaks are exacerbated for shallower summer mixed layers since the heat anomaly in the seasonal thermocline is larger relative to the heat anomaly stored in the summer mixed layer.

The spectrum of  $T$  for the reference case (Fig. B2, thick line) shows the expected frequency to the '-2' slope for frequencies below  $\epsilon(2\pi\rho_0c_pH_1)^{-1}$  (denoted by vertical thick line). Shallower summer thermoclines enhance the power at time scales of few years and shorter (dotted spectrum in Fig. B2), but do not affect the variance of SST at low frequencies. Furthermore, spectra of winter-centered, annual averages of SST faithfully reproduce the low frequency spectrum of  $T$  (not shown).

To explore the relationship between the damping rate  $\tilde{\alpha}$  derived from annual averaged values and the damping rates  $\epsilon(\rho_0c_pH)^{-1}$  for winter  $H = H_1$  and summer  $H = H_2$  (shown in Fig. B2 as the vertical, dotted line), equation (4) is fit to winter centered annual averages of the simulated  $T$  and  $\tilde{F} = Q$ . The estimate of  $\tilde{\alpha}$  is identical to the winter values for the reference run (dashed thick vertical line in Fig. B2). For cases II and III (not shown), the value of  $\alpha$  lies between the summer and winter damping rates, and is closer to the former. The exact dependence of the effective annual damping rate on the seasonal evolution of the mixed layer is nonlinear and complicated (see equation B1). For our purposes it suffices that the damping rate  $\tilde{\alpha}^{-1}$  is shorter than, but close to winter values.

## References

- Alexander, M. A., N.-C. Lau, and J. D. Scott, 2004: Broadening the atmospheric bridge paradigm: ENSO teleconnections to the North Pacific in summer and to the tropical west Pacific- Indian Oceans over the seasonal cycle. *In: Earth Climate: The Ocean-Atmosphere Interaction*, eds. C. Wang, S.-P. Xie and J. Carton. AGU **Monograph.**, 85-104.
- Alexander M. A., I. Blade, M. Newman, J. R. Lanzante, N. C. Lau, and J. D. Scott, 2002: The atmospheric bridge: The influence of ENSO teleconnections on air-sea interaction over the global oceans. *J. Climate*, **15**, 2205-2231.
- Alexander M. A., 1992: Midlatitude atmosphere-ocean interaction during El Niño. Part I: The North Pacific. *J. Clim.*, **5**, 944-958.
- An, S.-I. and B. Wang, 2005: The forced and intrinsic low-frequency modes of the North Pacific. *J. Climate*, **18**, in press.
- Barlow M., S. Nigam and E. H. Berbery, 2001: ENSO, Pacific decadal variability, and US summertime precipitation, drought, and stream flow. *J. Clim.*, **14**, 2105-2128.
- Barnett, T. P., D. W. Pierce, M. Latif, D. Dommenges and R. Saravanan, 1999a: Interdecadal interactions between the tropics and midlatitudes in the Pacific basin. *Geophys. Res. Lett.*, **26**, 615-618.
- Barnett, T. P., D. W. Pierce, R. Saravanan, N. Schneider, D. Dommenges and M. Latif, 1999b: Origins of the midlatitude Pacific decadal variability. *Geophys. Res. Lett.*, **26**, 1453-1456.

- Barnston A. G., Y. He and M. H. Glantz, 1999: Predictive Skill of Statistical and Dynamical Climate Models in SST Forecasts during the 1997-98 El Nino Episode and the 1998 La Nina Onset. *Bull. Am. Met. Soc.*, **80**, 217-244.
- Barsugli, J. J. and D. S. Battisti, 1998: The basic effects of atmosphere-ocean thermal coupling on mid-latitude variability. *J. Atmos. Sci.*, **55**, 477-493.
- Biondi F., A. Gershunov, and D. R. Cayan, 2001: North Pacific decadal climate variability since 1661. *J. Climate*, **14**, 5-10.
- Blade, I., 1997: The influence of midlatitude ocean-atmosphere coupling on the low-frequency variability of a GCM .1. No tropical SST forcing. *J. Clim.*, **10**, 2087-2106.
- Cayan D. R., M. D. Dettinger, H. F. Diaz and N. E. Graham, 1998: Decadal variability of precipitation over western North America. *J. Clim.*, **11**, 3148-3166.
- Chen D., M. A. Cane, A. Kaplan, S. E. Zebiak and D. J. Huang, 2004: Predictability of El Nino over the past 148 years. *Nature*, **428**, 733-736.
- Chelton, D. B., and R. E. Davis, 1982: Monthly mean sea-level variability along the west coast of North America. *J. Phys. Oceanogr.*, **12**, 757-784.
- Clarke, A. J., and A. Lebedev, 1999: Remotely driven decadal and longer changes in the coastal Pacific waters of the Americas. *J. Phys. Oceanogr.*, **29**, 828-835.
- Davis, R. E., 1976: Predictability of sea surface temperature and sea level pressure anomalies over the North Pacific Ocean. *J. Phys. Oceanogr.*, **6**, 249-266.
- Dettinger, M. D., D. R. Cayan, H. F. Diaz and D. M. Meko, 1998: North-south precipitation patterns in western North America on interannual-to-decadal timescales. *J. Clim.*, **11**, 3095-3111.



- Deser C., M. A. Alexander, and M. S. Timlin, 2003: Understanding the persistence of sea surface temperature anomalies in midlatitudes. *J. Climate*, **16**, 57-72.
- Deser, C., A. S. Phillips and J. W. Hurrell, 2004: Pacific interdecadal climate variability: Linkages between the tropics and North Pacific during boreal winter since 1900. *J. Climate*, **XX**, in press.
- Deser, C., M. A. Alexander and M. S. Timlin, 1999: Evidence for a wind-driven intensification of the Kuroshio Current Extension from the 1970s to the 1980s. *J. Climate*, **12**, 1697-1706.
- Dommenget, D., and M. Latif, 2002: Analysis of observed and simulated SST spectra in the midlatitudes. *Climate Dynamics*, **19**, 277-288.
- Evans, M. N., M. A. Cane, D. P. Schrag, A. Kaplan, B. K. Linsley, R. Villalba and G. M. Wellington, 2001: Support for tropically-driven Pacific decadal variability based on paleoproxy evidence. *Geophys. Res. Lett.*, **28**, 3689-3692.
- Frankignoul, C., P. Müller and E. Zorita, 1997: A simple model of the decadal response of the ocean to stochastic wind forcing. *J. Phys. Oceanogr.*, **27**, 1533-1546.
- Gedalof Z., N. J. Mantua and D. L. Peterson, 2002: A multi-century perspective of variability in the Pacific Decadal Oscillation: new insights from tree rings and coral. *Geophys. Res. Lett.*, **29**, Art. No. 2204.
- Garreaud, R. D. and D. S. Battisti, 1999: Interannual (ENSO) and interdecadal (ENSO-like) variability in the Southern Hemisphere tropospheric circulation. *J. Climate*, **12**, 2113-2123.

- Gershunov, A. and T. P. Barnett, 1998: Interdecadal modulation of ENSO teleconnections. *Bull. Amer. Met. Soc.*, **79**, 2715-2725.
- Graham, N. E., 1994: Decadal-scale climate variability in the tropical and North Pacific during the 1970s and 1980s - Observations and model results. *Clim. Dynam.*, **10**, 135-162.
- Hasselmann, K., 1976: Stochastic climate models. Part 1. Theory. *Tellus*, **26**, 473-485.
- Kalnay E., M. Kanamitsu, R. Kistler, W. Collins, D. Deaven, L. Gandin, M. Iredell, S. Saha, G. White, J. Woollen, Y. Zhu, M. Chelliah, W. Ebisuzaki, W. Higgins, J. Janowiak, K. C. Mo, C. Ropelewski, J. Wang, A. Leetmaa, R. Reynolds, R. Jenne and D. Joseph, 1996: The NCEP/NCAR 40-year reanalysis project. *Bull. Am. Meteorol. Soc.*, **77**, 437-471.
- Kushnir Y., W. A. Robinson, I. Blade, N. M. J. Hall, S. Peng and R. Sutton, 2002: Atmospheric GCM response to extratropical SST anomalies: Synthesis and evaluation. *J. Clim.*, **15**, 2233-2256.
- Krishnan, R. and M. Sugi, 2003: Pacific decadal oscillation and variability of the Indian summer monsoon rainfall. *Clim. Dyn.*, **21**, 233-242.
- Liebelt, P. B., 1967: An introduction to optimal estimation. *Addison-Wesley Pub. Co.*, **Reading, Mass.**, 273p.
- Lluch-Cota, D. B., W. S. Wooster and S. R. Hare, 2001: Sea surface temperature variability in coastal areas of the Northeastern Pacific related to the El Niño-Southern Oscillation and the Pacific Decadal Oscillation. *Geophys. Res. Lett.*, **28**, 2029-2032.
- Mantua, N.J, S. R. Hare, Y. Zhang, J. M. Wallace, and R.C. Francis, 1997: A Pacific interdecadal climate oscillation with impacts on salmon production. *Bull. Am. Met.*

- Soc.*, **78**, 1069-1079.
- Mantua N. J. and S. R. Hare, 2002: The Pacific decadal oscillation. *J. Oceanogr.*, **58**, 35-44.
- Minobe, S., 2000: Spatio-temporal structure of the pentadecadal variability over the North Pacific. *Prog. Oceanogr.*, **47**, 381-408.
- Miller, A. J., Cayan, D. R., Barnett, T. P., Graham, N. E., and Oberhuber, J. M., 1994: Interdecadal variability of the Pacific Ocean: Model response to observed heat flux and wind stress anomalies. *Clim. Dyn.*, **9**, 287-302..
- Miller, A. J., D. R. Cayan and W. B. White, 1998: A westward intensified decadal change in the North Pacific thermocline and gyre-scale circulation. *J. Climate*, **11**, 3112-3127.
- Miller, A. J. and N. Schneider, 2000: Interdecadal climate regime dynamics in the North Pacific Ocean: Theories, observations and ecosystem impacts. *Prog. Oceanogr.*, **27**, 257-260.
- Nakamura, H. and T. Yamagata, 1999: Recent decadal SST variability in the Northwestern Pacific and associated atmospheric anomalies. In. "*Beyond El Niño: Decadal and interdecadal climate variability*", **A. Navarra Ed., Springer Verlag, Berlin**, 49-72.
- Nakamura, H., and A. S. Kazmin, 2003: Decadal changes in the North Pacific oceanic frontal zones as revealed in ship and satellite observations. *J. Geophys. Res.*, **108**, Art. No. 3078.
- Nakamura, H., G. Lin and T. Yamagata, 1997: Decadal climate variability in the North Pacific during recent decades. *Bul. Am. Meteorol. Soc.*, **78**, 2215-2225.
- Nakamura, H., T. Izumi and T. Sampe, 2002: Interannual and decadal modulation recently observed in the North Pacific storm track activity and east Asian winter monsoon. *J.*

*Clim.*, **15**, 1855-1874.

Newman, M., G. P. Compo and M. A. Alexander, 2003: ENSO-forced variability of the Pacific decadal oscillation. *J. Clim.*, **16**, 3853-3857.

Nitta, T. and S. Yamada, 1989: Recent warming of tropical sea surface temperature and its relationship to the Northern Hemisphere circulation. *J. Meteor. Soc. Japan*, **67**, 375-383.

Pierce, D. W., 2002: The role of sea surface temperatures in interactions between ENSO and the North Pacific Oscillation. *J. Clim.*, **15**, 1295-1308.

Pierce, D. W., 2001: Distinguishing coupled ocean-atmosphere interactions from background noise in the North Pacific. *Prog. Oceanogr.*, **49**, 331-352.

Pierce, D. W., T. P. Barnett, N. Schneider, R. Saravanan, D. Dommenget and M. Latif, 2001: The role of ocean dynamics in producing decadal climate variability in the North Pacific. *Clim. Dyn.*, **18**, 51-70.

Pierce, D. W., T. Barnett and M. Latif, 2000: Connections between the Pacific Ocean tropics and midlatitudes on decadal time scales. *J. Climate*, **13**, 1173-1194.

Qiu, B., 2003: Kuroshio Extension variability and forcing of the Pacific decadal oscillations: Responses and potential feedback. *J. Phys. Oceanogr.*, **33**, 2465-2482.

Schneider, N. and A. J. Miller, 2001: Predicting Western North Pacific ocean climate. *J. Climate*, **14**, 3997-4002.

Schneider, N., A. J. Miller and D. W. Pierce, 2002: Anatomy of North Pacific decadal variability. *J. Climate*, **15**, 586-605.

- Seager, R., Y. Kushnir, N. Naik, M. A. Cane, and J. A. Miller, 2001: Wind-driven shifts in the latitude of the Kuroshio-Oyashio Extension and generation of SST anomalies on decadal timescales. *J. Climate*, **14**, 4249-4265.
- Sturges, W. and B. G. Hong, 1995: Wind forcing of the Atlantic thermocline along 32°N at low frequencies. *J. Phys. Oceanogr.*, **25**, 1706-1715.
- Tanimoto, Y., H. Nakamura, T. Kagimoto and S. Yamane, 2003: An active role of extratropical sea surface temperature anomalies in determining anomalous turbulent heat flux. *J. Geophys. Res.*, **108**, Art. No. 3304.
- Tomita, T., B. Wang, T. Yasunari and H. Nakamura, 2001: Global patterns of decadal-scale variability observed in sea surface temperature and lower-tropospheric circulation fields. *J. Geophys. Res.*, **106**, 26805-26815.
- Trenberth, K. E., 1990: Recent observed interdecadal climate changes in the Northern Hemisphere. *Bull. Am. Met. Soc.*, **71**, 988-993.
- Trenberth, K. E. and J. W. Hurrell, 1994: Decadal atmosphere-ocean variations in the Pacific. *Clim. Dyn.*, **9**, 303-319.
- Vimont, D. J., D. S. Battisti, and A. C. Hirst, 2003: Seasonal Footprinting in the Pacific: Implications for ENSO. *J. Clim.*, **16**, 2668-2675.
- Vimont, D. J., D. S. Battisti and A. C. Hirst, 2001: Footprinting: A seasonal connection between the tropics and mid-latitudes. *Geophys. Res. Lett.*, **28**, 3923-3926.
- Xie, S. P., T. Kunitani, A. Kubokawa, M. Nonaka and S. Hosoda, 2000: Interdecadal thermocline variability in the North Pacific for 1958-1997: A GCM simulation. *J. Phys. Oceanogr.*, **30**, 2798-2813.

Yulaeva, E., N. Schneider, D. W. Pierce and T. Barnett, 2000: Modeling of North Pacific climate variability forced by oceanic heat fluxes anomalies. *J. Climate*, **14**, 4027-4046.

Zhang, Y., J.M. Wallace and D.S. Battisti, 1997: ENSO-like interdecadal variability: 1900-93. *J. Clim.*, **10**, 1004-1020.

---

## Figure Captions

**Fig. 1.** Time series of monthly values of the PDO (top, thin line), and of PDO based on July to June annual averages of SSTA (top, thick line). The correlation of annual averages of the monthly values of the PDO, and of the PDO estimated from annual averages of SSTA is 0.99, and the latter is used in this study. The lower panels show monthly values of  $\tilde{F}_i(t)$  of NINO3.4, NPI,  $P_{DEL}$  and  $P_{AVG}$ . All time series are normalized to unit standard deviation. The dotted lines in the lower two panels denote  $P_{DEL}$  and  $P_{AVG}$  obtained from North Pacific wind stress curl that had the regression with low pass time series of NINO3.4 and NPI removed.

**Fig. 2.** PDO pattern from observations (top), derived as the leading EOF of the reconstructed SSTA (center) and from the reconstruction obtained with a spatially constant value of  $\tilde{\alpha}$ . The magnitude depicts the SSTA in °K for a unit deviation of the principal component, contour level is 0.2, with negative contours dotted.

**Fig. 3.** Correlation times 10 of observed and reconstructed PDO time evolution, with a contour interval of 1. At every location, the PDO is fit to and reconstructed from an AR-1 process of equation (1), forced by the local sea level pressure time series. High correlation indicates regions in which sea level pressure anomalies are most influential to the observed PDO. Top panel shows results for full sea level pressure, lower panel results for sea level pressure with NINO3.4 temperature index removed. The removal is achieved by subtracting the (least square fit) linear regression of anomalous sea level pressure and NINO3.4. Dithering in the North Pacific marks the area of spatial average used to estimate the NPI index.

**Fig. 4.** Significance levels (95%) of the correlation of 50 year hindcast of (top) observed SSTA and best fit AR-1 model forced by red noise time series. The lower panels show the 95% significance levels for the contributions of NINO3.4, NPI,  $P_{DEL}$  and  $P_{AVG}$ . The significance levels are based on one thousand reconstructions of SSTA, and includes the effect of artificial skill from the selection used in deriving some of the forcing indices. Contour interval is 0.1.

**Fig. 5.** Correlation times 10 of 50 year AR-1 model SSTA hindcast and observed July to June averages of SSTA (top). The lower panels show the correlation of observed and hindcast SSTA using only forcing by (respectively) NINO3.4, NPI,  $P_{DEL}$  and  $P_{AVG}$ . Contour interval is 2.



**Fig. 6.** Time series of July to June annual averages of PDO (top, black line). Overlaid in gray is the PDO reconstruction based on SSTA reconstruction (top). The lower panels show  $F_i(t)$  for NINO3.4, NPI,  $P_{AVG}$  and  $P_{DEL}$ . Thin solid lines denote the spatial averages of the filtered index time series, and tiny vertical bars their spatial standard deviation. Dashed lines show the rotated time series  $F_i(t)^*$ , and the thick gray lines denote their projection onto the observed pattern of the PDO (see equation (7)). All time series have been normalized to unit standard deviation.

**Fig. 7.** Estimate of damping time  $\tilde{\alpha}^{-1}$  of equation (3) in months. Contour interval is 10 months.

**Fig. 8.** Forcing footprints  $\gamma_i(x, y)$  of NINO3.4 (top) and NPI (bottom). The maps represent the response of SST in  $^{\circ}\text{K}$  after the forcing of unit magnitude has been applied for one year. Contour interval is 0.1, negative contours are dotted.

**Fig. 9.** Regression pattern with Kuroshio-Oyashio Extension circulation indices of zonal advection (top) and thermocline depth (bottom). Units are  $^{\circ}\text{K}$ , and correspond to the response of SST after the forcing of unit magnitude has been applied for one year. Contour interval is 0.1, negative contours are dashed, and the zero contour is omitted. Thin dotted lines indicate the areas used in the calculation of the indices. Contour interval is 0.1, negative contours are dotted.

**Fig. 10.** Rotated footprints for  $\gamma_i(x, y)^*$  of NINO3.4\* (top) and NPI\* (bottom). The maps represent the response of SST in  $^{\circ}\text{K}$  after the forcing of unit magnitude has been applied for one year. Contour interval is 0.1, negative contours are dotted.

**Fig. 11.** The PDO time series (top) and reconstruction (top, gray) based on equation (7). The lower panels show the contributions to the PDO from NINO3.4\*, NPI\* and  $P_{DEL}^*$ . The index for thermocline depth estimate  $P_{AVG}^*$  does not explain a significant fraction of the SSTA variability anywhere, and is therefore deemed insignificant for the reconstruction of the PDO. Dotted vertical lines mark the winters of 1976/77 and 1998/99.

**Fig. 12.** Power spectrum as a function of frequency in cycles/year of the observed and reconstructed PDO, and its contributions  $(\omega^2 + \alpha_0^2)^{-1} \gamma_i^2 P_i^2$  due to NPI\*, NINO34\* and  $P_{DEL}^*$  (as indicated). The solid black line denotes the spectrum of the observed PDO, the light gray line with black center that of the reconstruction. Spectra have been smoothed by three successive applications of a 5 point running mean. Fluctuations of the spectra for frequencies above  $0.6 \text{ cyc yr}^{-1}$  are not significant.

**Fig. B1.** Autocorrelation of SST based on the idealized reemergence model, equation (B1,) for  $H_1 = 100m$  and  $H_2 = 40m$ . The x-axis denotes the month, with winter occupying months 1 through 6, and summer the remainder of the year. The y axis denotes the lag in months. Contour level is 0.2.

**Fig. B2.** Spectrum of the simulated SST based on equation (B1) for the reference run  $H_1 = H_2 = 100m$  (without re-emergence, solid thick line), and with  $H_2 = 40m$  (dotted spectrum). The damping time scale for winter mixed layer is marked by the solid vertical line, while the damping time scale for the summer mixed layer is shown as dotted vertical lines. The dashed lines correspond to the damping rate  $\tilde{\alpha}$  derived from winter centered, annual averaged data, for the summer mixed layer depth  $H_2 = 40m$ , and for the model without reemergence ( $H_2 = H_1$ ).

	$\alpha(x)$	$\alpha_0$	$\alpha_0$ , no temporal covariance	$\alpha_0$ , NINO3.4*, NPI* only
Pattern	0.98	0.98	0.98	0.98
Principal component	0.93	0.93	0.93	0.89

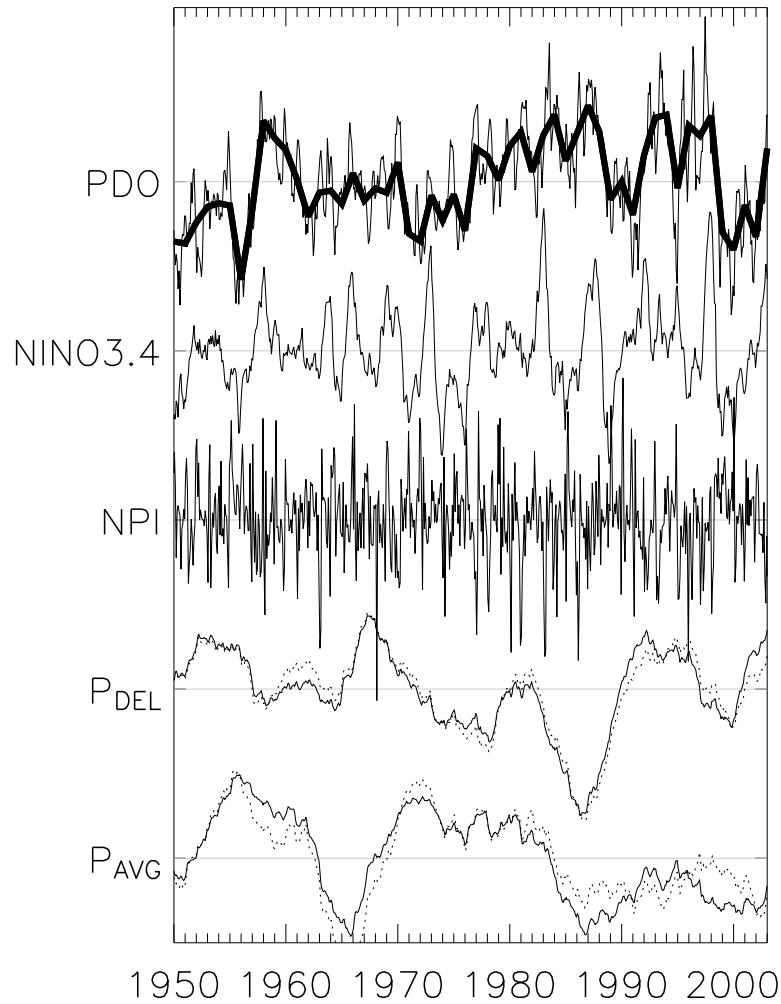
**Table 1.** Correlation coefficients of observed PDO patterns (top row) and principal component (bottom row) with leading EOF of the SSTA reconstruction using spatially varying  $\alpha$  (column 1) or constant  $\alpha_0$  (column 2). Column 3 shows the results obtained from setting the off-diagonal elements of the covariance matrix of the forcing indices to zero, and column 4 shows results from considering only the forcing by NINO3.4\* and NPI\*.

	NINO3.4*	NPI*	$P_{DEL}^*$	$P_{AVG}^*$
NINO3.4	1	0	0	0
NPI	-0.55	0.83	0	0
$P_{DEL}$	0.10	0.07	0.99	0
$P_{AVG}$	-0.07	-0.03	0.24	0.97

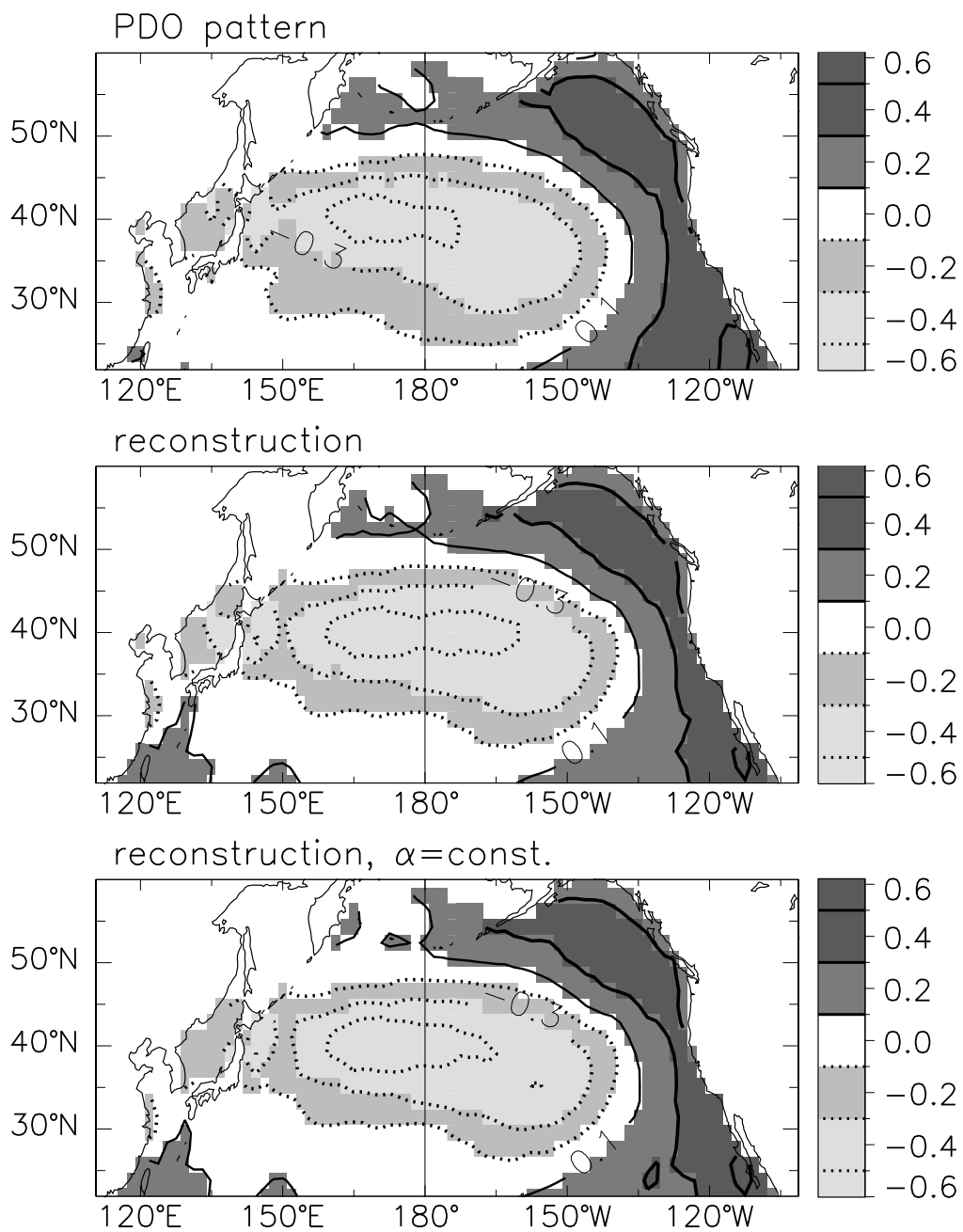
**Table 2.** Rotation matrix  $B_{ij}$  that converts the forcing time series  $F_i$ , denoted by the leftmost column, to the orthogonal forcing time series  $F_j^*$ , denoted by top row. The original and rotated time series are all normalized to unit standard deviations, so that the variance accounted for by  $F_j^*$  is given by the square of the values of the table. The values are the spatial mean of the rotation matrix at every location, however, the spatial variations are very small, the standard deviation of the non-zero elements are of the order of 0.001 or smaller.

	$\langle \alpha \Phi_k \Phi_0 \rangle$				$\langle \gamma_i \Phi_0 \rangle$			
	k= 0	1	2	...	NINO3.4	NPI	$P_{DEL}$	$P_{AVG}$
SSTA reconstruction	0.26	-0.004	-0.03	<O(0.03)	0.19	-0.68	-0.17	-0.05
forcing orthogonalized					0.55	-0.57	-0.18	-0.05
Observed PDO	0.22				0.20	-0.68	-0.19	-0.05
forcing orthogonalized					0.56	-0.58	-0.20	-0.05

**Table 3.** Coefficients of equation (7) governing the PDO evolution estimated from the fit of the observed SSTA evolution to equation (4). The first row shows the projection onto observed patterns of the PDO; column one depicts the the autoregressive parameter of the PDO amplitude, rows 2-4 shows the coupling to higher observed EOFs. The last four columns shows the coefficients multiplying the forcing indices corresponding to NINO3.4, NPI,  $P_{DEL}$  and  $P_{AVG}$ . The second row shows results for the forcing fields orthogonalized with matrix  $B_{ij}$ . All forcing time series were normalized to unit variance. Rows 3 and 4 show the results from fitting the observed time evolution of the PDO to equation (7) while neglecting the coupling to the other EOFs.

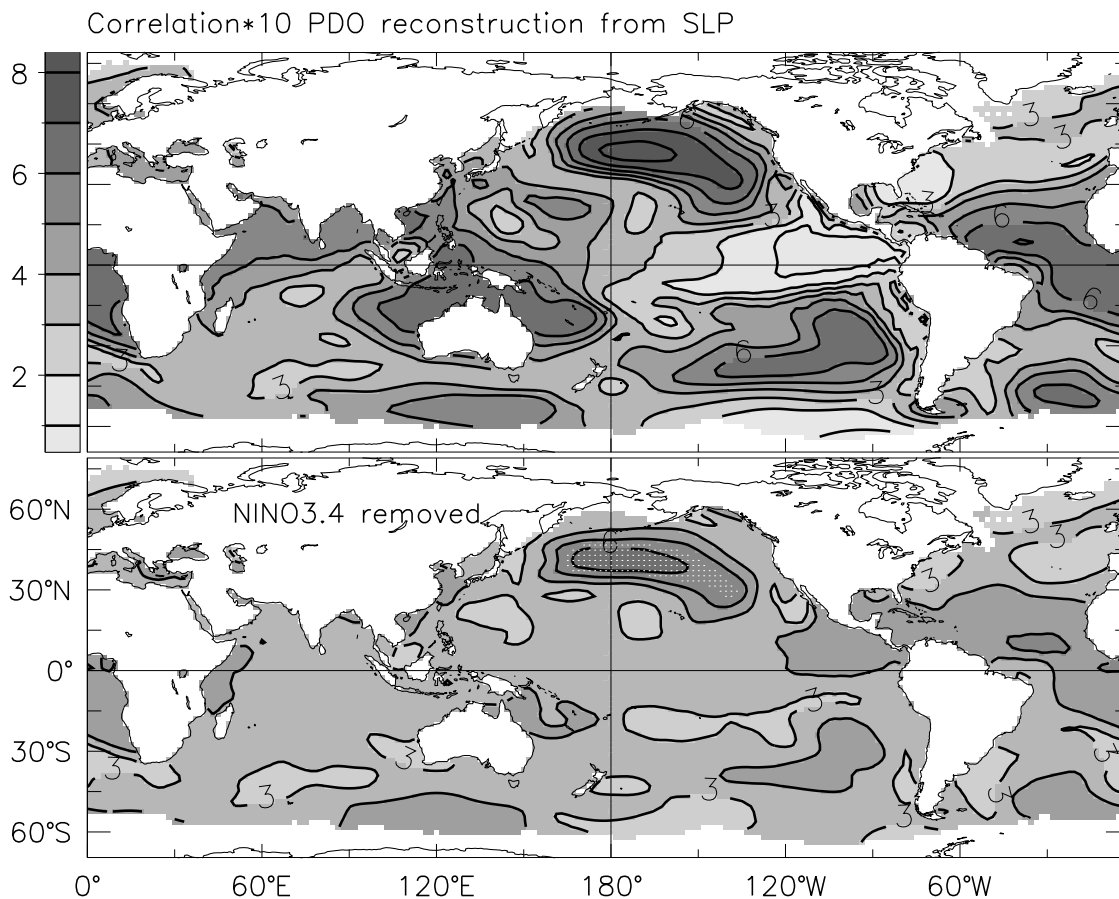


**Fig. 1.** Time series of monthly values of the PDO (top, thin line), and of PDO based on July to June annual averages of SSTA (top, thick line). The correlation of annual averages of the monthly values of the PDO, and of the PDO estimated from annual averages of SSTA is 0.99, and the latter is used in this study. The lower panels show monthly values of  $\tilde{F}_i(t)$  of NINO3.4, NPI,  $P_{DEL}$  and  $P_{AVG}$ . All time series are normalized to unit standard deviation. The dotted lines in the lower two panels denote  $P_{DEL}$  and  $P_{AVG}$  obtained from North Pacific wind stress curl that had the regression with low pass time series of NINO3.4 and NPI removed.

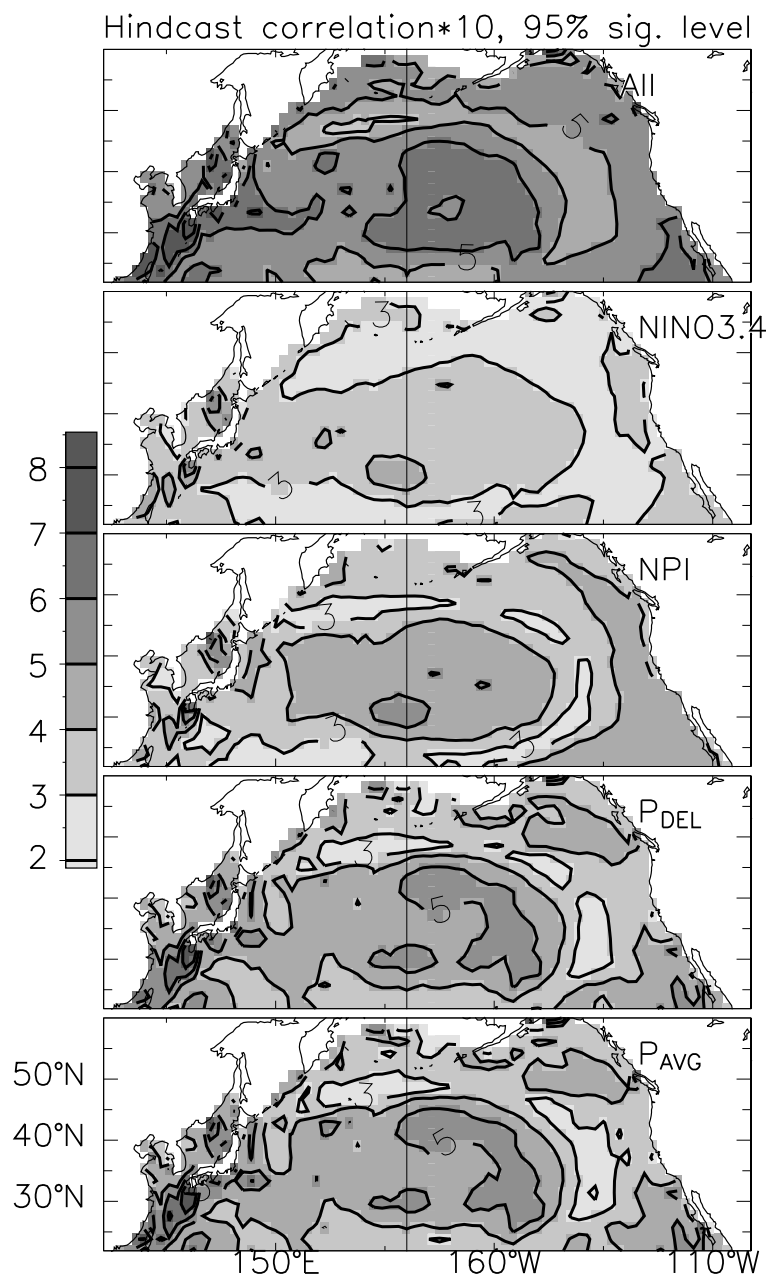


**Fig. 2.** PDO pattern from observations (top), derived as the leading EOF of the reconstructed SSTA (center) and from the reconstruction obtained with a spatially constant value of  $\tilde{\alpha}$ . The magnitude depicts the SSTA in °K for a unit deviation of the principal component, contour level is 0.2, with negative contours dotted.

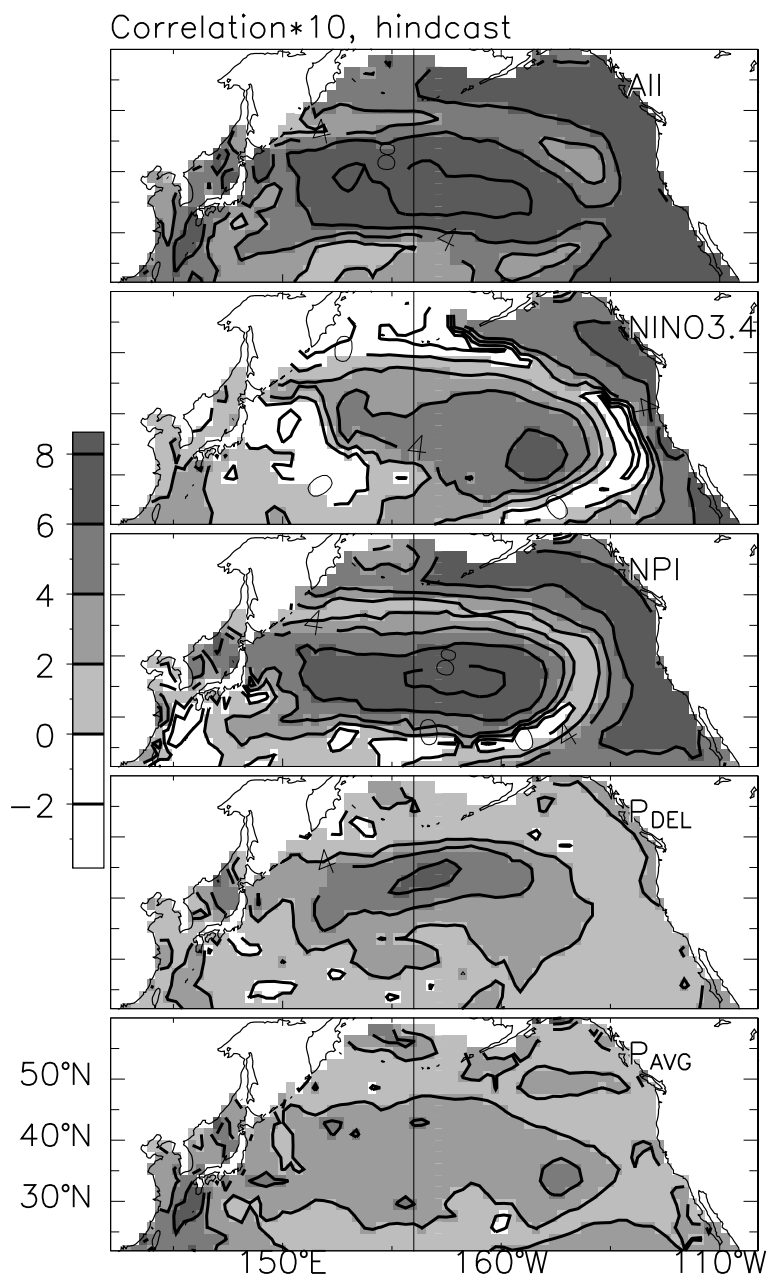




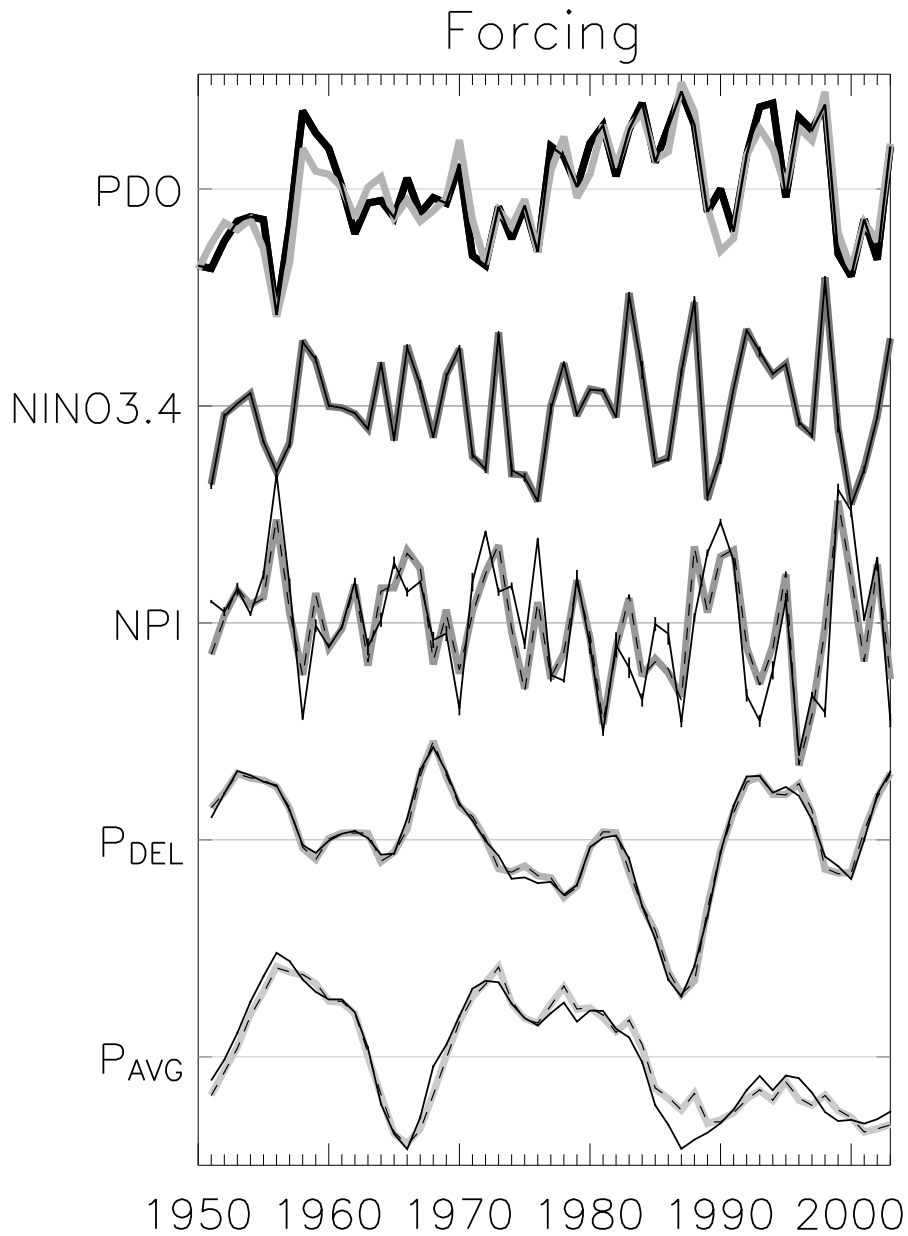
**Fig. 3.** Correlation times 10 of observed and reconstructed PDO time evolution, with a contour interval of 1. At every location, the PDO is fit to and reconstructed from an AR-1 process of equation (1), forced by the local sea level pressure time series. High correlation indicates regions in which sea level pressure anomalies are most influential to the observed PDO. Top panel shows results for full sea level pressure, lower panel results for sea level pressure with NINO3.4 temperature index removed. The removal is achieved by subtracting the (least square fit) linear regression of anomalous sea level pressure and NINO3.4. Dithering in the North Pacific marks the area of spatial average used to estimate the NPI index.



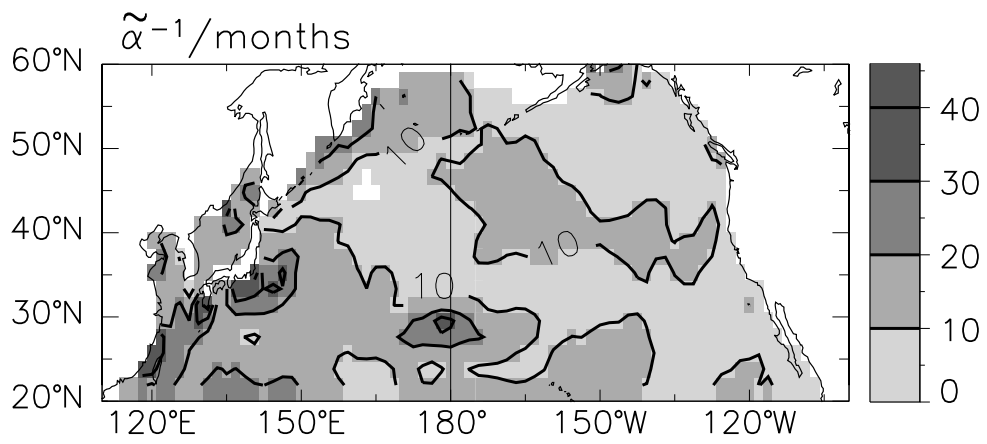
**Fig. 4.** Significance levels (95%) of the correlation of 50 year hindcast of (top) observed SSTA and best fit AR-1 model forced by red noise time series. The lower panels show the 95% significance levels for the contributions of NINO3.4, NPI,  $P_{DEL}$  and  $P_{AVG}$ . The significance levels are based on one thousand reconstructions of SSTA, and includes the effect of artificial skill from the selection used in deriving some of the forcing indices. Contour interval is 0.1.



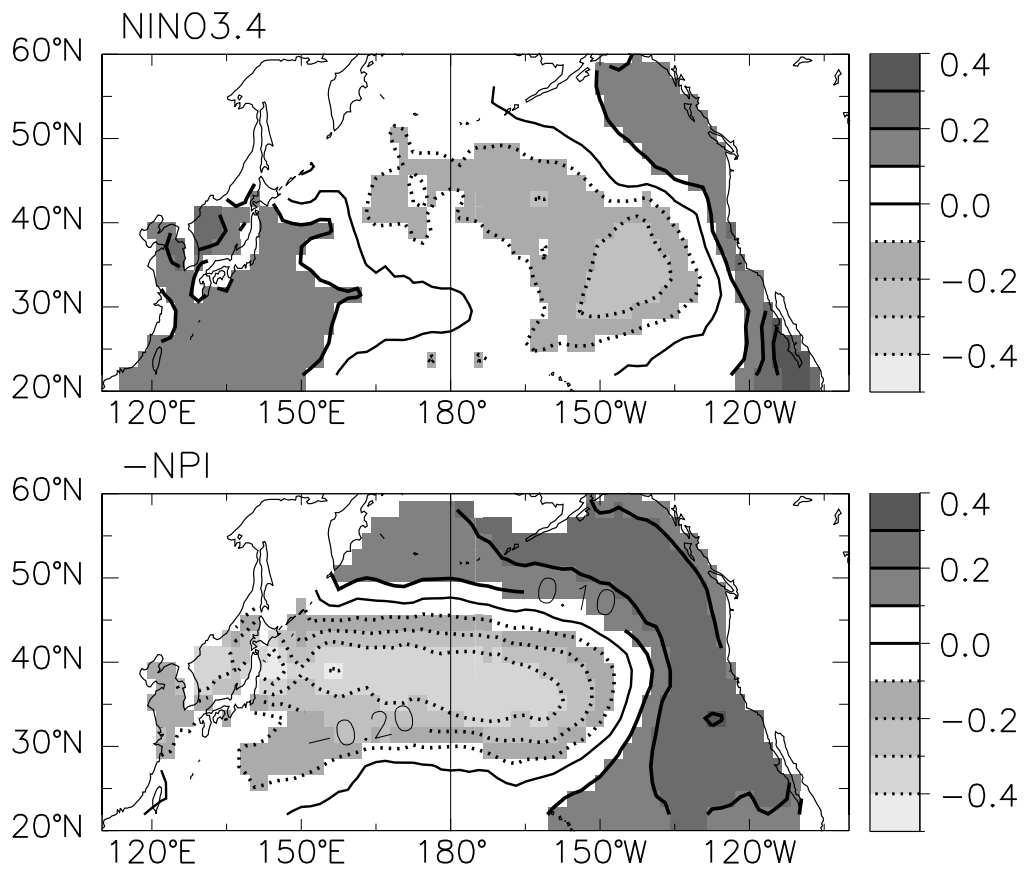
**Fig. 5.** Correlation times 10 of 50 year AR-1 model SSTA hindcast and observed July to June averages of SSTA (top). The lower panels show the correlation of observed and hindcast SSTA using only forcing by (respectively) NINO3.4, NPI,  $P_{DEL}$  and  $P_{AVG}$ . Contour interval is 2.



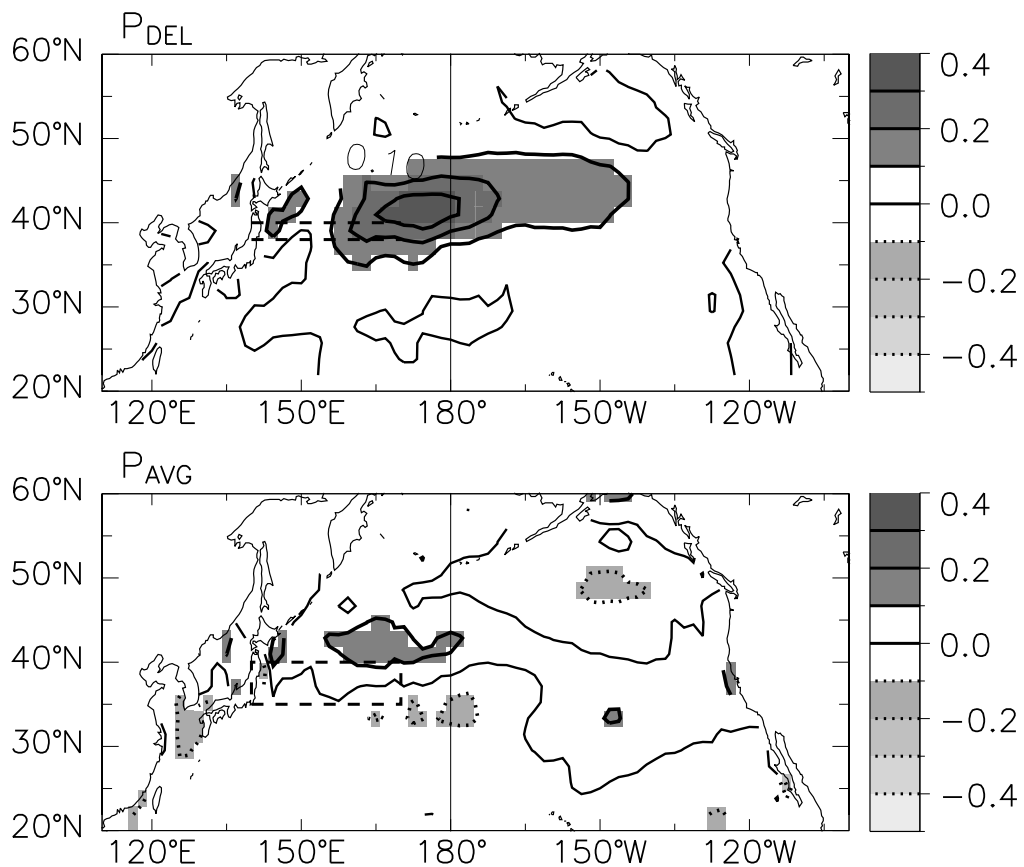
**Fig. 6.** Time series of July to June annual averages of PDO (top, black line). Overlaid in gray is the PDO reconstruction based on SSTA reconstruction (top). The lower panels show  $F_i(t)$  for NINO3.4, NPI,  $P_{AVG}$  and  $P_{DEL}$ . Thin solid lines denote the spatial averages of the filtered index time series, and tiny vertical bars their spatial standard deviation. Dashed lines show the rotated time series  $F_i(t)^*$ , and the thick gray lines denote their projection onto the observed pattern of the PDO (see equation (7)). All time series have been normalized to unit standard deviation.



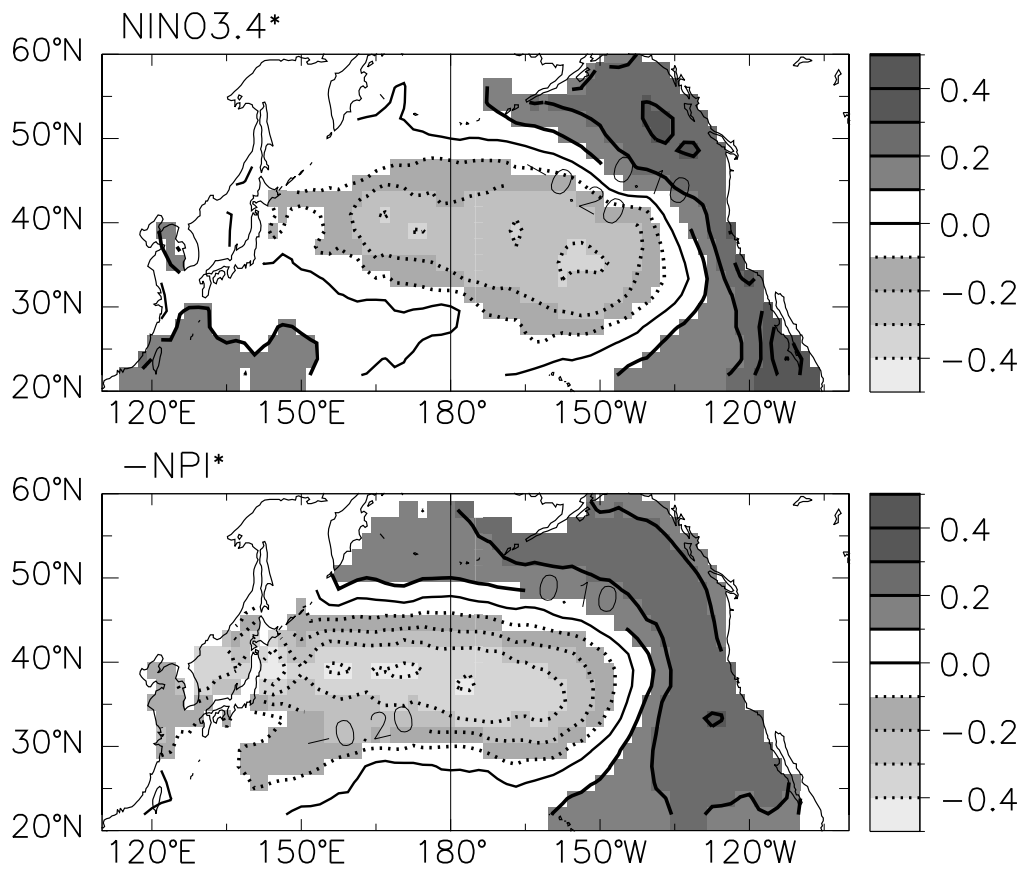
**Fig. 7.** Estimate of damping time  $\tilde{\alpha}^{-1}$  of equation (3) in months. Contour interval is 10 months.



**Fig. 8.** Forcing footprints  $\gamma_i(x, y)$  of NINO3.4 (top) and NPI (bottom). The maps represent the response of SST in  $^{\circ}\text{K}$  after the forcing of unit magnitude has been applied for one year. Contour interval is 0.1, negative contours are dotted.

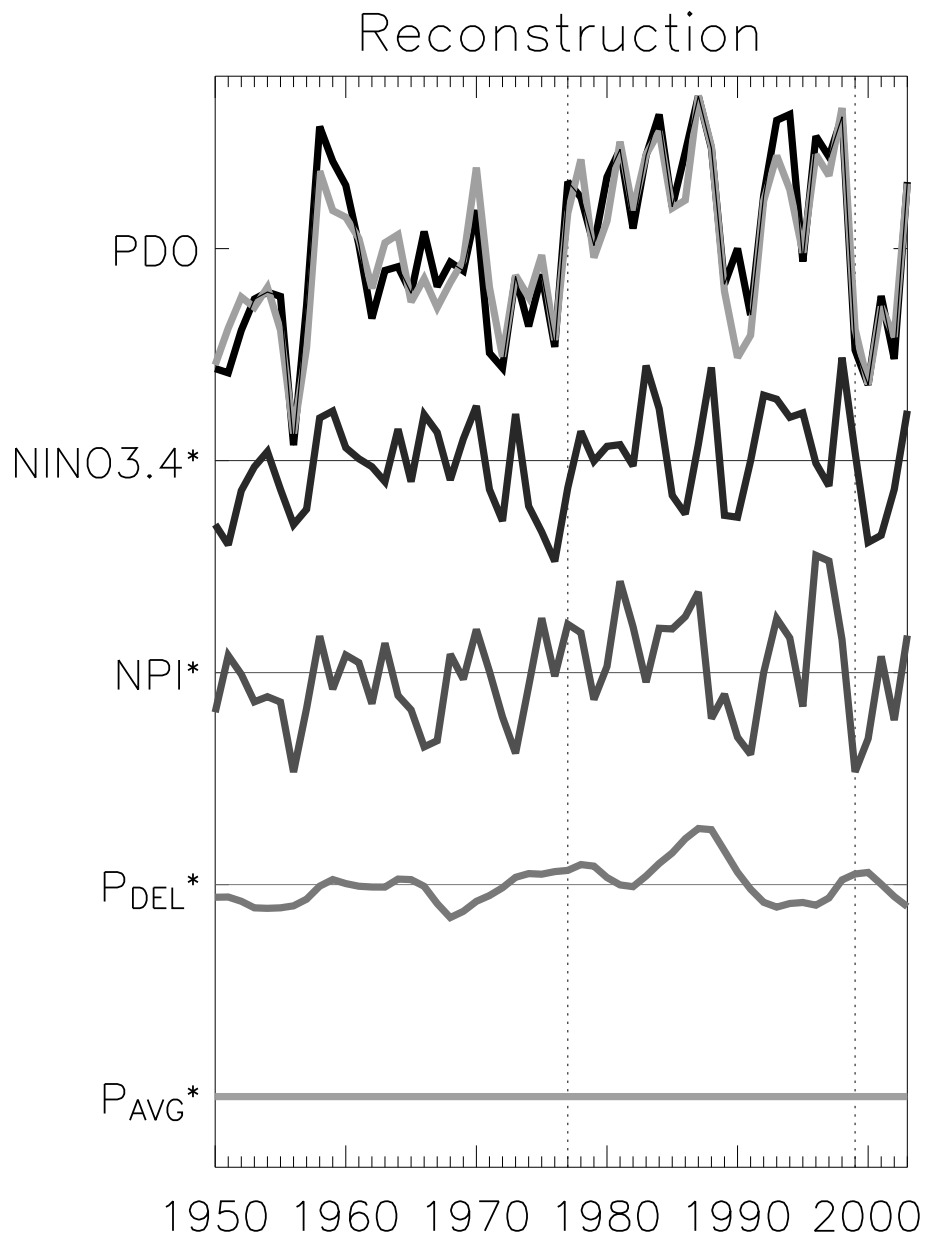


**Fig. 9.** Regression pattern with Kuroshio-Oyashio Extension circulation indices of zonal advection (top) and thermocline depth (bottom). Units are  $^{\circ}\text{K}$ , and correspond to the response of SST after the forcing of unit magnitude has been applied for one year. Contour interval is 0.1, negative contours are dashed, and the zero contour is omitted. Thin dotted lines indicate the areas used in the calculation of the indices. Contour interval is 0.1, negative contours are dotted.

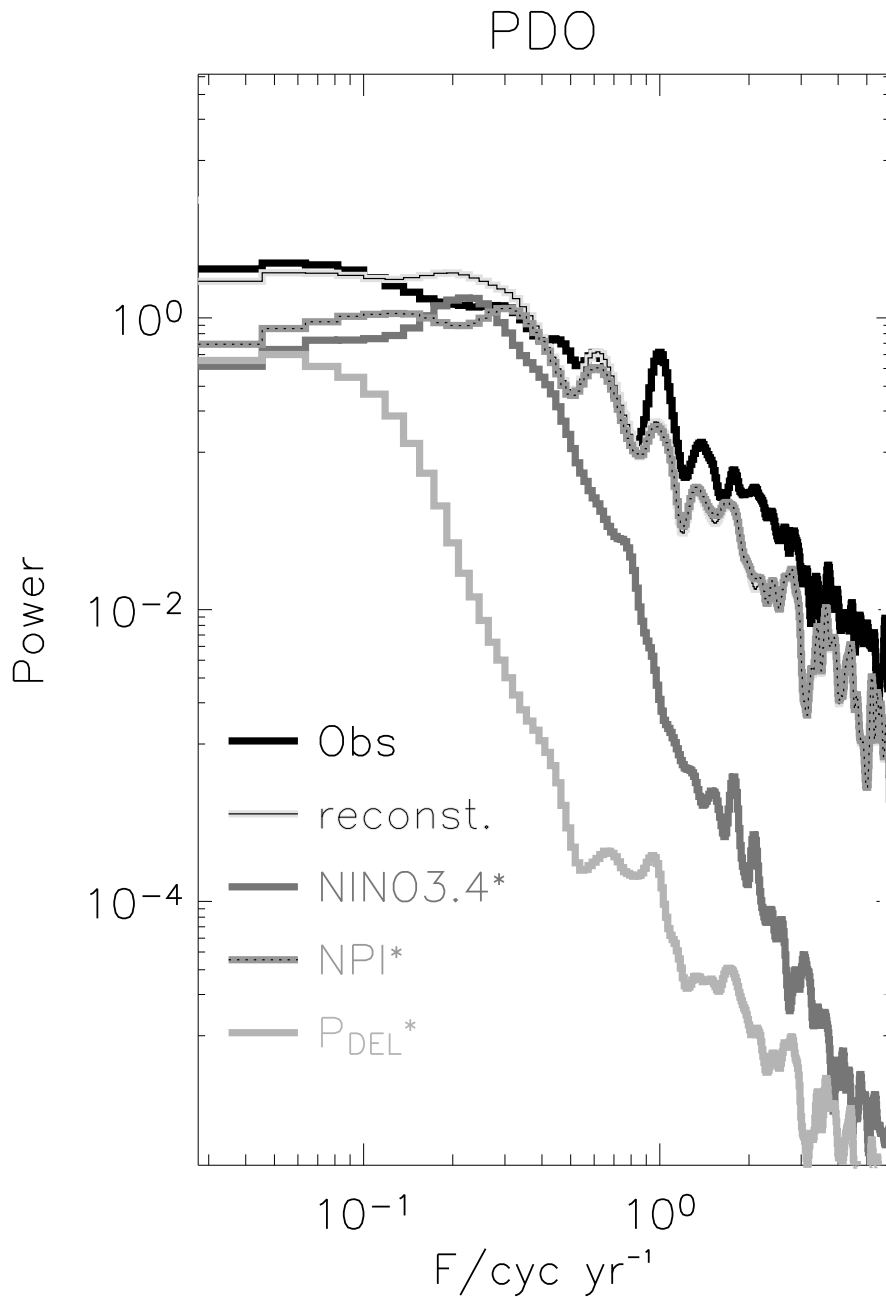


**Fig. 10.** Rotated footprints for  $\gamma_i(x, y)^*$  of NINO3.4\* (top) and NPI\* (bottom). The maps represent the response of SST in °K after the forcing of unit magnitude has been applied for one year. Contour interval is 0.1, negative contours are dotted.

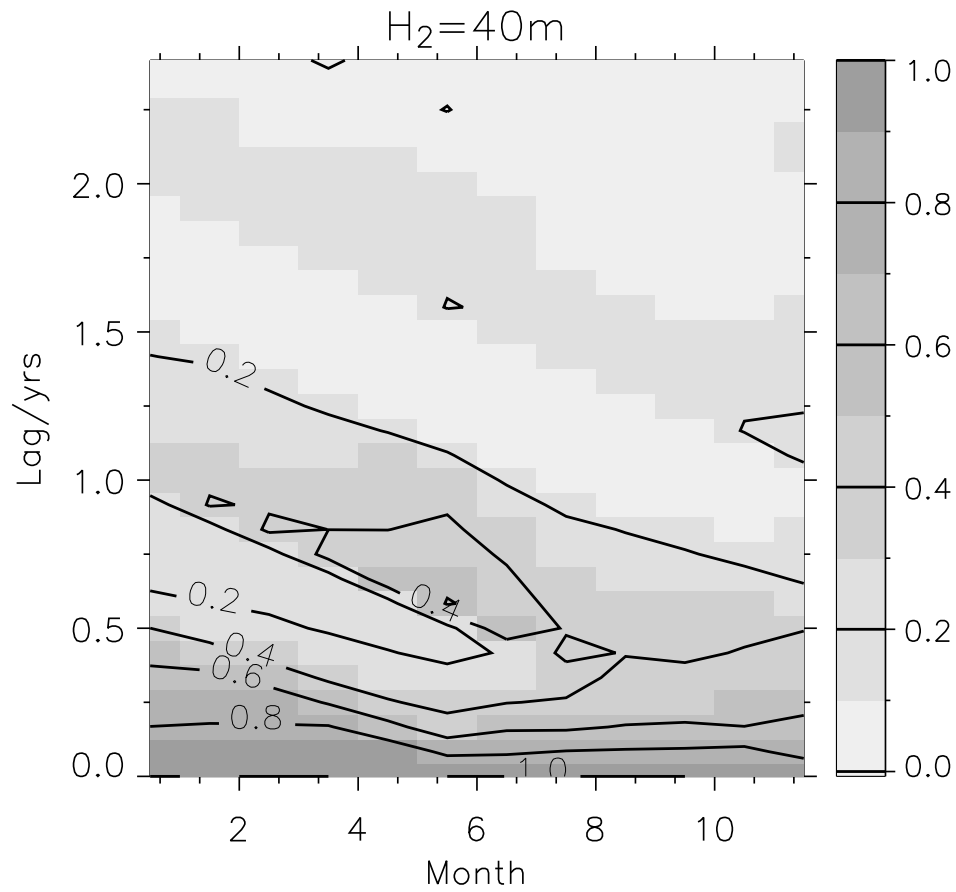




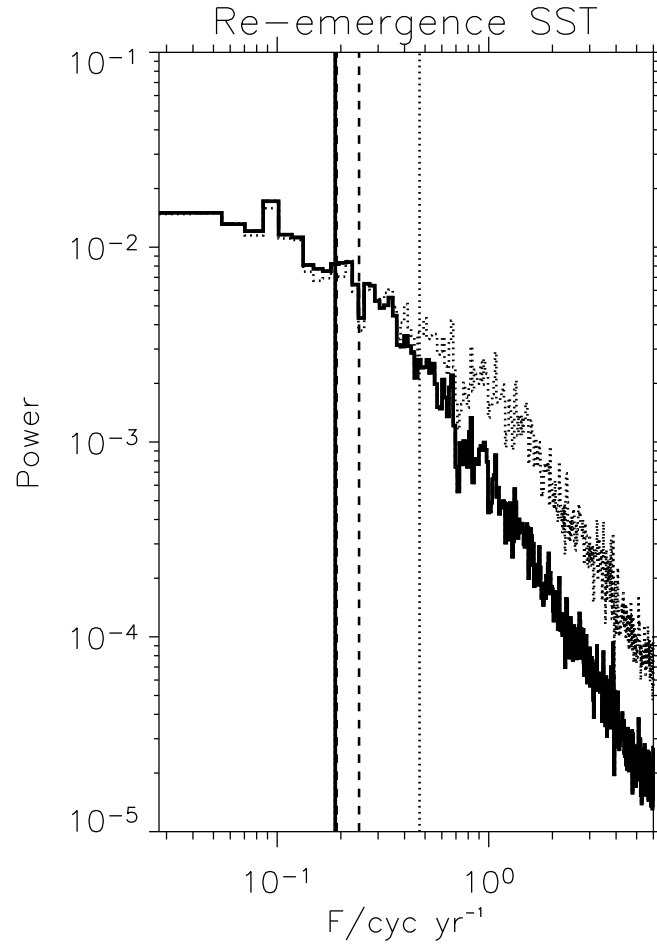
**Fig. 11.** The PDO time series (top) and reconstruction (top, gray) based on equation (7). The lower panels show the contributions to the PDO from NINO3.4\*, NPI\* and  $P_{DEL}^*$ . The index for thermocline depth estimate  $P_{AVG}^*$  does not explain a significant fraction of the SSTA variability anywhere, and is therefore deemed insignificant for the reconstruction of the PDO. Dotted vertical lines mark the winters of 1976/77 and 1998/99.



**Fig. 12.** Power spectrum as a function of frequency in cycles/year of the observed and reconstructed PDO, and its contributions  $(\omega^2 + \alpha_0^2)^{-1} \gamma_i^2 P_i^2$  due to NPI\*, NINO34\* and  $P_{DEL}^*$  (as indicated). The solid black line denotes the spectrum of the observed PDO, the light gray line with black center that of the reconstruction. Spectra have been smoothed by three successive applications of a 5 point running mean. Fluctuations of the spectra for frequencies above  $0.6 \text{ cyc yr}^{-1}$  are not significant.



**Fig. B1.** Autocorrelation of SST based on the idealized reemergence model, equation (B1,) for  $H_1 = 100m$  and  $H_2 = 40m$ . The x-axis denotes the month, with winter occupying months 1 through 6, and summer the remainder of the year. The y axis denotes the lag in months. Contour level is 0.2.



**Fig. B2.** Spectrum of the simulated SST based on equation (B1) for the reference run  $H_1 = H_2 = 100m$  (without re-emergence, solid thick line), and with  $H_2 = 40m$  (dotted spectrum). The damping time scale for winter mixed layer is marked by the solid vertical line, while the damping time scale for the summer mixed layer is shown as dotted vertical lines. The dashed lines correspond to the damping rate  $\tilde{\alpha}$  derived from winter centered, annual averaged data, for the summer mixed layer depth  $H_2 = 40m$ , and for the model without reemergence ( $H_2 = H_1$ ).