# **Role of Vertical Mixing Originating From Small Vertical Scale Structures above and within the Equatorial Thermocline in an OGCM**



#### Abstract

30 31 Recent high vertical resolution measurements show small vertical scale structures (SVSs) 32 of the shear of ocean current are present above and within the equatorial thermocline. We 33 investigate the impact of the mixing induced by the SVSs on the state of the equatorial 34 Pacific in an ocean general circulation model (OGCM). The SVSs are typically 35 unresolved in OGCMs and thus their impact needs to be parameterized. As a first step to 36 determine the importance of the SVS induced mixing we introduce an enhanced mixing 37 within and above the equatorial thermocline. It is found that this enhanced mixing 38 reduces the stratification above the thermocline, and sharpens the thermocline through the 39 Phillips effect [*Phillips*, 1973]. The sharpened thermocline limits the exchange of heat 40 across the thermocline and traps the surface heating above the thermocline. The reduced 41 stratification leads to less cooling of the mixed layer through entrainment, a reduced 42 annual cycle and an increase in the annual mean of the sea surface temperature (SST) in 43 the eastern equatorial cold tongue. The depth dependency in enhanced SVS mixing is 44 crucial to its impact. When the enhanced mixing is applied throughout the depth of the 45 ocean the cold tongue SST is cooled further. In the western equatorial Pacific, where the 46 thermocline is deeper, SVS enhanced mixing induces a colder SST. We also find that the 47 SVS mixing reduces the eddy kinetic energy associated with the tropical instability waves 48 through a reduction of the meridional and vertical shear of the equatorial currents and 49 temperature gradient.

# 51 **1. Introduction**





93 equatorial thermocline. The vertical mixing originating from the SVSs, therefore, needs

- 94 to be parameterized and its impact investigated. In this study, as a first step towards
- 95 gaining an understanding of the likely role of SVS induced mixing in the dynamics of the

96 equatorial ocean we employ a simple method for parameterization of the SVS mixing,

97 and focus on the impacts of the SVS mixing on the climatological state of the equatorial 98 Pacific.

99 The rest of this paper is structured as follows: the OGCM is introduced in section 100 2 and we describe the experimental design, Section 3 presents the effects of SVS mixing 101 on the equatorial Pacific, and Section 4 provides summary and discussions.

### 102 **2. Model Description and Experimental Design**

#### 103 **2.1. OGCM**

104 The OGCM used in this study is the NEMO modeling system [*Madec*, 2006], 105 which includes the ocean model Océan Parallélisé (OPA9). We employ the ORCA-R05 106 grid, which has a global configuration grid at 0.5˚cos(lat) resolution. The OPA9 with the 107 ORCA-R05 grid has 31 vertical levels with the first 14 levels lying in the top 150 meters. 108 Oceanic vertical eddy diffusivity and viscosity coefficients are calculated from a 1.5- 109 order turbulent closure scheme [*Blanke and Delecluse*, 1993]. In the turbulent closure 110 scheme, the background vertical diffusivity coefficient is defined as the lower limit of the 111 vertical diffusion coefficient. We retain this technique of specifying the background 112 diffusivity in the experiments reported here, but note that specifying the background 113 diffusivity by "adding" a value to the calculated value of the diffusion coefficient does 114 not unduly affect the results (in the case of SST, the impact of changing the way the 115 background diffusivity is specified is found to be an order of magnitude smaller than that 116 of changing the value of the diffusivity itself). 117 The atmospheric forcing for the OGCM experiments is taken from the CORE

118 (Coordinated Ocean-ice Reference Experiments) normal year forcing based on the

119 NCEP/NCAR reanalysis [*Large and Yeager*, 2004]. We utilize the following variables; 6- 120 hourly varying 10m air temperature, specific humidity, and zonal and meridional marine 121 wind vectors, daily varying surface downward shortwave and longwave radiation, and 122 monthly varying rain and snow. The latent and sensible heat fluxes are calculated from 123 the bulk formula according to the *Large and Yeager* [2004].

124 The model is initialized by setting the temperature and salinity equal to *Levitus*  125 [1982], and a state of the rest. We have integrated the OGCM for 15 years, and analyzed 126 the climatological annual mean for the last 5 years using output of 5-day means (we find 127 that the ten year spin-up is sufficient for the tropical ocean to reach an equilibrium). Two 128 experiments were integrated for a further 5 years (CTL and DEP20\_LEV05, see below) 129 and daily-mean output generated to allow an investigation of the impact of the SVS 130 mixing on the eddy heat advection associated with tropical instability waves (TIWs), 131 described in section 3.3.

#### 132 **2.2. Parameterization of SVS Mixing and Experimental Design**

133 We have performed simulations with and without parameterized SVS mixing. 134 Only the background vertical diffusivity coefficients are different between the 135 simulations.

136 For the control run (CTL: without SVS mixing), the background vertical 137 diffusivity coefficient is set to be a constant  $1.0 \times 10^{-6}$  m<sup>2</sup>s<sup>-1</sup> throughout the water column 138 in the whole computational domain. The low value for the background vertical diffusivity 139 coefficient is chosen because of the observation of low values at low latitudes [*Gregg et*  140 *al.*, 2003].



164 increased linearly from DEP=15<sup>°</sup>C to a value of  $1 \times 10^{-4}$  m<sup>2</sup>s<sup>-1</sup> at the base of the mixed 165 layer (see LEVvar in Table 1). We note that our experiments differ from those of *Meehl*  166 *et al.* [2001] and *Richards et al.* [2009] who consider a constant background vertical 167 diffusivity. In our case the background diffusivity is allowed to vary with depth. As we 168 will see, this variation with depth has a large impact on the model solution.

169 **3. Results** 

170 We briefly evaluate the OGCM performance in terms of the capturing the 171 observed annual mean and annual cycle of SST, and annual mean of zonal currents in the 172 tropical Pacific.

173 Fig. 2a shows the annual mean SST for the tropical Pacific in the CTL. The warm 174 pool SST (WPSST) and the cold tongue SST (CTSST) are well simulated. However, the 175 CTSST in the run without SVS mixing (CTL) is up to approximately 1˚C too cold (red 176 line in Fig. 3a). On the other hand, the WPSST in the run without SVS mixing is 177 positively biased by about  $0.5^{\circ}$ C (red line in Fig. 3a). These positive and negative SST 178 biases lead to a steeper zonal gradient of SST along the equatorial Pacific. Comparing the 179 amplitude of the annual cycle in CTL at 0˚N, 120˚W with observations we find that the 180 modeled SST annual cycle is greater than that of observed (red and black dotted lines in 181 Fig. 3b). The modeled SST in Fig. 3b contains the intra-monthly variability since the 182 output interval of the model is kept at 5-day. On the other hand the observed SST lacks 183 the intra-seasonal variability since the dataset is monthly averaged. Even allowing for the 184 strong intra-seasonal variability in the modeled SST, the modeled SST in the eastern 185 equatorial Pacific is negatively biased particularly during July-February (Fig. 3b). The 186 observed small amplitude of the annual cycle of SST in the western equatorial Pacific is

187 well simulated (Fig. 3b), even though the modeled SST is positively biased throughout 188 the year.

189 The 20°C isotherm depth, representing the thermocline depth, and the 16°C and 190 22<sup>°</sup>C isotherms, whose depth difference is used as a measure of the thickness of the 191 thermocline, are shown in Fig. 2b for CTL and observation. The thermocline depth 192 shoaling toward the east in the equatorial Pacific is reasonably well simulated as observed. 193 The thermocline depth in the CTL is shallower than that observed. On the other hand, the 194 thermocline thickness in the eastern equatorial Pacific in the CTL is comparable to that 195 observed. The shallower thermocline is consistent with the stronger annual cycle of SST 196 in the eastern equatorial Pacific, since it is easier for equatorial upwelling to tap the 197 colder sub-thermocline water with shallower thermocline for a given wind variation 198 [*Meehl et al.*, 2001] (as seen in Fig. 3b). 199 Figs. 2d and e compare the annual mean of zonal current along the equatorial

200 Pacific between observation and CTL. The jet-like structure of the equatorial 201 undercurrent (EUC) is well simulated as observed, although the magnitude of the 202 modeled EUC is up to  $0.2 \text{ ms}^{-1}$  stronger than that of observed. In association with the too-203 strong EUC, the modeled westward surface current is weaker than that of observed (Figs. 204 2d and e). The too-strong EUC in the CTL might be due to lack of lateral diffusivity 205 originating from the interleaving process in the OGCM [*Pezzi and Richards*, 2003]. 206 In summary, SST in the equatorial Pacific is qualitatively well simulated by the 207 CTL of our OGCM, although the modeled SST in the equatorial Pacific is biased to some 208 extent compared to the observed SST in terms of the annual mean and the amplitude of 209 the annual cycle. The EUC is also well simulated by CTL of our OGCM in terms of the

210 structure, although the magnitude of the modeled EUC is too strong compared to that 211 observed. In the next section, impacts of SVS mixing on SST in the equatorial Pacific are 212 described.

#### 213 **3.1 Impact of SVS mixing on the annual mean**

214 Fig. 4 shows differences in the annual mean of SST simulated by the OGCM with 215 and without SVS mixing. SSTs in the equatorial Pacific, Costa Rica Dome [*Wyrtki*, 1964], 216 and the coastal region of Peru are strongly affected by the SVS mixing. The annual mean 217 of the CTSST simulated by the OGCM with SVS mixing, except DEP0\_LEV05, is 218 warmer than that without SVS mixing, while the WPSST simulated by the OGCM with 219 SVS mixing is colder than that without SVS mixing. SSTs in the Costa Rica Dome and 220 the coastal region of Peru have also become warmer by the SVS mixing. 221 The CTSST in DEP20\_LEV05 is warmer than that in CTL by up to  $1\degree$ C (Fig. 4a). 222 On the other hand, the CTSST in DEP0\_LEV05 run is colder than that in CTL (Fig. 4c). 223 The DEP15 LEV05 (i.e. when SVS mixing is applied down to the  $15\degree C$  isotherm) is 224 approximately at the transition point between the CTSST being warmed and being cooled 225 by the SVS mixing (Fig. 4b). We find, therefore, that the warming of the CTSST in 226 simulations with SVS mixing is reduced as the depth to which SVS mixing is applied is 227 deepened. A SST warming in the Costa Rica Dome and the coastal region of Peru is not 228 excessively affected by changing the depth to be which SVS mixing is applied (Figs. 4a, 229 b, and c).

230 The cooling of the CTSST found in the DEP0\_LEV05 (Fig. 4c) is a typical 231 response to elevated background vertical diffusivity throughout the water column. More 232 specifically, the elevated background vertical mixing throughout the water column brings 233 up the cold, deeper waters and reduces the temperature in the upper ocean. Such a cooling 234 of the CTSST by elevated background vertical diffusivity throughout the water column is 235 also simulated in a regional atmosphere-ocean coupled model [*Richards et al.*, 2009]. 236 The marked difference in the SST response between DEP20 LEV05 and 237 DEP0\_LEV05 when SVS mixing is introduced highlights the importance of the vertical 238 distribution of the enhanced mixing.

239 For a fixed vertical distribution (DEP=20 $^{\circ}$ C) the warming in the CTSST and a 240 cooling of the WPSST are enhanced as the magnitude of the SVS mixing is elevated 241 (Figs. 4a, d, and e). The warming of SST in the Costa Rica Dome and the coastal region 242 of Peru is also enhanced as the magnitude of the SVS mixing is elevated (Figs. 4a, d, and 243 e).

244 There is also a marked difference in the annual mean of SST between

245 DEP15\_LEV05 and DEP15\_LEVvar (Figs. 4b and f), even though the isotherm-depth

246 mean of the background vertical diffusivity coefficient for both runs are nearly equal to

247 each other. A cooling of the WPSST is dominant in DEP15\_LEV05 (Fig. 4b), while a

248 warming of the CTSST is significant in DEP15\_LEVvar (Fig. 4g). We discuss the cause

249 of the difference in SST between the two runs in section 3.3.

250 The changes to the subsurface temperature and zonal component of velocity along 251 the equator induced by SVS mixing are shown in Fig. 5 (the CTL is shown in Fig. 2).

252 Quantitative measures of the depth of the  $20^{\circ}$ C isotherm and thermocline thickness at 3

253 longitudes are given in Table 2 for all experiments. There are marked differences in the

254 changes depending on the depth where the enhanced mixing is specified. With a depth

255 independent enhancement (DEP0\_LEV05) there is a general broadening of the

256 thermocline and associated cooling/warming above/below the  $20\degree C$  isotherm. When the 257 SVS mixing is restricted to above the 20˚C, the thermocline sharpens and there is a 258 general warming of the thermocline. The reasons for the sharpening of the thermocline 259 are discussed in section 3.3. In the eastern half there is a warming throughout the water 260 column above the thermocline.

261 Table 3 provides quantitative measures of the position of the core of the EUC at 3 262 longitudes for all experiments. There is a general deepening of the core of the EUC. For a 263 fixed vertical distribution (DEP=20 $^{\circ}$ C) the core of the EUC in the eastern equatorial 264 Pacific is deepened as the magnitude of the SVS mixing is elevated. With a depth 265 independent enhancement (DEP0\_LEV05), there is a broadening of the EUC and 266 associated strengthening/weakening in the lower/upper part of the EUC (Fig. 5f), which 267 is a typical response to the elevated vertical mixing throughout the water column. 268 Restricting the SVS mixing depth to be above the 20˚C isotherm, there is a deepening of 269 the EUC (Table 3) and associated strengthening in the lower part of the EUC (Fig. 5d).

#### 270 **3.2 Changes in the Annual Cycle of SST**

271 Does a warming of the annual mean of the CTSST (Fig. 4) in simulations with 272 SVS mixing take place throughout the year? To answer this question, we investigate 273 changes in the annual cycle of SST along the equatorial Pacific. Fig. 2c shows the annual 274 cycle of SST along the equatorial Pacific simulated in CTL. A warming of the CTSST 275 during boreal spring associated with both the passage of solar zenith and reduced cloud 276 cover during the period [*Kessler et al.*, 1998] is well simulated by the ocean model. Fig. 277 6a shows a difference in the annual cycle of SST along the equatorial Pacific between 278 DEP20 LEV05 and CTL. A warming of the CTSST exceeds 1<sup>°</sup>C during July-February,

279 while a warming of the CTSST during March-June is much less. This result reveals that 280 the warming of the annual mean of the CTSST in DEP20 LEV05 (Fig. 4a) is due to a 281 SST warming during the second half of the year (July-February). A warming of the 282 CTSST during the second half of the year is also found in other simulations with SVS 283 mixing (Fig. 6).

284 On the other hand, the CTSST during boreal spring-summer in DEP15 LEV05 285 and DEP0\_LEV05 is colder than that in CTL (Figs. 6b and c). This result reveals that the 286 colder annual mean of SST in DEP15\_LEV05 and DEP0\_LEV05 (Figs. 4b and c) is due 287 to the cooling during boreal spring-summer (Figs. 6b and c). 288 Hereafter, we mainly focus on the DEP20\_LEV05, DEP20\_LEV1, and

289 DEP0\_LEV05 to compare the impact of the magnitude of SVS mixing and the depth to 290 which it is applied.

#### 291 **3.3. Changes in Mixed Layer Heat Budget in the Cold Tongue**

292 To understand the mechanism of changes in the CTSST caused by SVS mixing, 293 we examine the heat budget of the mixed layer (ML) in the eastern equatorial Pacific 294 (2°S-2°N, 160°W-80°W). The ML temperature  $(T_m; MLT)$  evolution is given by the 295 following equation [e.g. *Menkes et al.*, 2006].

$$
\frac{\partial T_m}{\partial t} = -\langle u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} + w \frac{\partial T}{\partial z} \rangle + \langle D_t(T) \rangle
$$

296  

$$
-\frac{1}{h}\frac{\partial h}{\partial t}[T-T(z=h)]+\frac{1}{h}(K_z\frac{\partial T}{\partial z})(z=h)+\frac{Q_*-Q_s[1-f(z=h)]}{\rho_0C_p h}
$$
 (1)

297 where the angle brackets denote a vertical average over the depth of the ML, *h*. The ML 298 depth (MLD) is calculated as the depth where the density is 0.05 kg m<sup>-3</sup> higher than the

299 surface density as used in *Menkes et al.* [2006] and *Cravatte and Menkes* [2009]. In Eq. 300 (1), term A (advection term) represents the advection of temperature by horizontal and 301 vertical currents, term B represents the lateral diffusion, and term C (vertical diffusion 302 term) represents the exchanges between the ML and the deeper ocean. The last term 303 includes the diffusive flux term and entrainment through the ML base. The term D 304 (atmospheric forcing term) represents the net surface heat flux absorbed by the ML. In 305 our experiments, the entrainment is calculated as the residual between the left-hand side 306 in Eq. (1) and terms A, B, D, and the diffusive flux term.

307 Fig. 7a shows the annual cycle of the term A, B, C and D for the ML in the cold 308 tongue in CTL. A warming by the surface heat fluxes and a cooling by the vertical 309 diffusion are balanced as shown in earlier studies [*Menkes et al.*, 2006; *Cravatte and*  310 *Menkes*, 2009]. The lateral diffusion term is negligible throughout the year. Temperature 311 tendency shows significant intra-monthly variability particularly during boreal fall. The 312 intra-monthly variability of the temperature tendency coincides well with that of the 313 advection term. The intra-monthly variation of the advection term is related to the TIW 314 activity [*Cravatte and Menkes*, 2009]. The impact of SVS mixing on the TIW activity is 315 discussed in section 3.5.

316 In the experiments with depth dependent SVS mixing (DEP20\_LEV05 and 317 DEP20\_LEV1) there is a reduced warming by the atmospheric fluxes and a reduced 318 cooling by vertical diffusion (Figs. 7b and d). The reduced atmospheric forcing is due to a 319 warmer MLT which induces greater loss of latent heat, longwave radiation, and sensible 320 heat. Therefore the reduction of the atmospheric forcing is the result rather than the cause 321 of the SST warming. These results indicate that the warming of the CTSST in simulations

322 with SVS mixing is induced by a reduction in diffusion in the second half of the year. For 323 instance, the vertical diffusion term in DEP20\_LEV1 is around −0.1˚C/day during 324 August-November (Fig. 7d), while that in CTL is less than −0.2˚C/day (Fig. 7a). A 325 weakening of the cooling by vertical diffusion during August-November is also seen in 326 DEP20\_LEV05 (Fig. 7b).

327 Fig. 8 shows the atmospheric forcing, advection, and vertical diffusion terms for 328 the ML of the cold tongue averaged for the second half of the year. The warming by 329 atmospheric fluxes is balanced with a cooling by vertical diffusion in the time averaging 330 (right and left parts of Fig. 8). On the other hand, the advection term averaged for the 331 second half of the year is negligible (central part of Fig. 8). There is a notable reduction 332 in the cooling by vertical diffusion when depth dependent SVS mixing is applied, with 333 the reduction increasing with the level of enhanced mixing. This clearly indicates that the 334 warmer MLT during the second half of the year in the DEP20 runs is caused by a 335 reduction of vertical diffusion. This is in stark contrast to the colder cold tongue and 336 increased cooling by vertical diffusion when the enhanced mixing is applied throughout 337 the depth of the water column (green bar in Fig. 8).

338 Fig. 9 shows the atmospheric forcing, advection, and vertical diffusion terms for 339 the ML of the CT averaged for the first half of the year (March-June). Now advection 340 plays a somewhat larger role (although it is still small). The changes induced by depth 341 dependent SVS mixing are much less than those in the second half of the year, while 342 those induced by depth independent enhanced mixing are somewhat greater.

343 In summary, a warmer CTSST during the second half of the year in simulations 344 with depth dependent SVS mixing is caused by a weaker cooling associated with 345 weakened vertical diffusion.

346 The vertical diffusion term consists of the entrainment and diffusive flux terms. 347 The entrainment term is negligible compared to the diffusive flux term in our experiments (Figure not shown). The diffusive flux,  $\frac{1}{h}(K_z \frac{\partial I}{\partial z})_{z=h}$  $K_z \frac{\partial T}{\partial x}$  $h^{(\mathbf{R}_z)}\partial z^{j_z}$ 348 (Figure not shown). The diffusive flux,  $\frac{1}{2}(K, \frac{\partial T}{\partial y})_{z=h}$ , depends on the MLD (*h*), vertical diffusivity coefficient  $(K_z)$ , and vertical gradient of temperature ( *z T* ∂ 349 diffusivity coefficient ( $K_z$ ), and vertical gradient of temperature ( $\frac{\partial T}{\partial z}$ ) at the ML base. 350 From the formulation of the diffusive flux, it is obvious that a thicker ML, weaker 351 vertical gradient of temperature, and weaker vertical mixing contribute less to cool the 352 MLT. Fig. 10a shows the annual cycle of the stratification (in terms of the square of the 353 buoyancy frequency), mixed layer depth and depth of the 20˚C isotherm averaged 354 between 2˚S- 2˚N, 120˚W-100˚W for the CTL. A particular feature to note is the 355 shoaling of the thermocline in the second half of the year. Figs. 10b and d show the 356 changes in the stratification and vertical diffusivity when depth limited SVS mixing is 357 introduced. The enhanced mixing above the thermocline produces a sharpening of the 358 thermocline and a much-reduced stratification (and vertical temperature gradient) above 359 the thermocline. The reduced stratification leads to an increase in the vertical diffusivity 360 which feeds back to further reduce the stratification and tighten the thermocline (the so-361 called "Phillips effect"; *Phillips*, 1972). The reduced stratification (and warmer 362 temperature, recall Fig. 5) allows the deepening of the mixed layer in the second half of 363 the year, and produces a reduced cooling of the mixed layer because of the reduced

364 temperature gradient and warmer temperature (Fig. 5a), despite the increase in vertical 365 diffusivity.

366 The increase in vertical diffusivity associated with the reduction of the 367 stratification leads to a reduction of the magnitude of the upper part of the EUC (Fig. 5d). 368 The reduction of the magnitude of the upper EUC reduces the vertical shear of the current, 369 which in turn reduces the vertical diffusivity in the layer. This reduction of the upper 370 EUC, therefore, works to weaken the Phillips effect to some extent. In contrast, a depth 371 independent increase in the background mixing (DEP0\_LEV05; Fig. 10c) weakens the 372 thermocline and brings cooler water to the base of the mixed layer (Fig. 5c). This has the 373 effect of slightly reducing the depth of the mixed layer and increasing the cooling of the 374 mixed layer through vertical diffusion (again, despite the decrease in vertical diffusivity). 375 Fig. 11 shows the background vertical diffusivity coefficients for the 376 DEP20\_LEV05, DEP15\_LEV05 and DEP15\_LEVvar. The background vertical 377 diffusivity for the DEP15\_LEVvar is much closer to that of the DEP20\_LEV05 (changes 378 in SST in DEP15\_LEVvar are also closer to those in DEP20\_LEV05 than to 379 DEP15\_LEV05, recall Fig. 4). In case of DEP15\_LEVvar, a relatively strong SVS 380 mixing above the thermocline induces the Phillips effect to deepen and sharpen the 381 thermocline and to increase the CTSST, while relatively weak SVS mixing below the 382 thermocline does not bring up the cold water to diffuse the thermocline. 383 **3.4. Changes in Mixed Layer Heat Budget in the Warm Pool**  384 Fig. 12 shows the annual cycle of the tendency terms for the ML heat budget in 385 the western equatorial Pacific in the CTL and SVS runs. The annual mean of the various

386 terms is shown in Fig. 13. The atmospheric forcing and vertical diffusion terms show two

387 peaks during boreal spring and autumn (Fig. 12), which are due to the passage of the 388 solar zenith. Advection contributes to cool the mixed layer. Introducing SVS enhanced 389 mixing leads to an increase in the cooling due to vertical diffusion and advection. Note 390 that the cooling occurs for both the depth dependent and independent cases.

391 Fig. 14 shows the annual cycle of stratification, mixed layer depth, depth of the 392 20°C isotherm and vertical diffusivity in the western equatorial Pacific for the CTL. The 393 thermocline depth in the WP is much deeper and the annual cycle is much weaker than 394 that in the CT (Figs. 10 and 14). Fig. 14c shows the changes in the stratification and 395 vertical diffusivity when depth independent SVS mixing (DEP0\_LEV05) is introduced. 396 The depth independent SVS mixing weakens the thermocline and brings cooler water to 397 the base of the mixed layer. The mechanism of the cooling of WPSST is the same as that 398 of a cooling of CTSST (section 3.3).

399 Figs. 14b and d show the changes in the stratification and vertical diffusivity 400 when depth limited SVS mixing is introduced. The SVS enhanced mixing above the 401 thermocline sharpens the thermocline and a much-reduced stratification above the 402 thermocline. The vertical diffusivity above the mixed layer depth is much reduced, while 403 stratification is not changed much. The difference in SST response to the depth limited 404 SVS mixing between WP and CT may be due to the distance between the mixed layer 405 and the thermocline. In fact the response of the CTSST is weak from March to June 406 during which the thermocline is deep.

#### 407 **3.5. Impact of SVS mixing on Tropical Instability Waves**

408 Although SVS mixing does not affect an advection term in the ML in the eastern 409 equatorial Pacific during the second half of the year (central part of Fig. 8), it is

410 interesting to understand impacts of SVS mixing on the eddy advection associated with 411 TIW activity. To evaluate impacts of the SVS mixing on the eddy advection, an 412 advection term is decomposed into the following four terms; the advection of mean 413 temperature by mean current  $\overline{U}$  $\overline{V}$ , the advection of eddy temperature by mean 414 current ( $-\overline{U}\nabla T'$ ), the advection of mean temperature by eddy current ( $-U'\nabla T$ ), and the 415 advection of eddy temperature by eddy current  $(-U'\nabla T')$ , where  $\overline{U} = (\overline{u}, \overline{v}, \overline{w})$  and 416  $U'=(u',v',w')$  denote the mean and the eddy current field, respectively.  $\overline{T}$  and  $T'$ 417 represents the mean and eddy temperatures, respectively.  $(u \frac{\partial T}{\partial t} + v \frac{\partial T}{\partial t} + w \frac{\partial T}{\partial t}) = -UVT - UVT' - U' \nabla T - U' \nabla T'$ *z*  $w \frac{\partial T}{\partial x}$ *y*  $v \frac{\partial T}{\partial x}$ *x*  $u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} + w \frac{\partial T}{\partial y} = -\overline{U} \nabla \overline{T} - \overline{U} \nabla T - U' \nabla \overline{T} - U' \nabla T$ ∂  $+w\frac{\partial}{\partial x}$ ∂  $+\nu\frac{\partial}{\partial}$ ∂ 418  $-(u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} + w \frac{\partial T}{\partial y}) = -\overline{U} \nabla \overline{T} - \overline{U} \nabla T - U' \nabla \overline{T} - U' \nabla T'$  (2) 419 The mean field is obtained by applying a 70-day running-mean filter to daily mean field 420 from a 5-yr simulation. The eddy field is obtained by subtracting the mean field from the 421 daily mean field. The mean advection term −*U*∇*T* therefore represents the advection of 422 low-frequency temperature by low-frequency currents. The eddy advection term 423 representing the effects of eddies is defined as  $-\overline{U}\nabla T'$ - $U'\nabla \overline{T}$  −  $U'\nabla T'$ . 424 Fig. 15a shows the annual mean of the eddy kinetic energy (EKE) averaged from the surface to 100m depth. The EKE is defined as  $\frac{1}{2} \rho_0 (U^2 + V^2)$ 2 425 the surface to 100m depth. The EKE is defined as  $\frac{1}{2}\rho_0(U^{2}+V^{2})$ , where  $\rho_0$  is the 426 density. The EKE of the CTL has a peak at  $2°-4°N$  in the eastern equatorial Pacific, as 427 simulated in *Small et al.* [2009]. The EKE of DEP20\_LEV05 is weaker than that of the 428 CTL (Fig. 15b).

429 Fig. 16 shows the monthly means of the mean and eddy advection terms in the 430 eastern equatorial Pacific for CTL and DEP20\_LEV05. The mean advection term is

431 negative throughout the year, indicating that the mean advection tends to cool the MLT in 432 the eastern equatorial Pacific. In contrast, the eddy advection warms the MLT in the 433 eastern equatorial Pacific particularly during boreal summer and autumn (Fig. 14). These 434 results are consistent with results based on observations [*Wang and McPhaden*, 1999; 435 *Jochum et al*., 2007] and OCGM experiments [*Cravatte and Menkes*, 2009; *Richards et*  436 *al*, 2009]. The introduction of SVS mixing reduces the cooling due to the mean advection, 437 particularly during the second half of the year, when compared to the CTL. This reduced 438 cooling by the mean advection is compensated by a reduced warming by the eddy flux. 439 As a result, SVS mixing reduces the amplitude of the annual cycle of both the mean and 440 eddy advective heat fluxes, while producing virtually no change to the total advective 441 heat flux (Figs. 8 and 9). The changes in mean and eddy fluxes are explained by changes 442 in barotropic (BT) and baroclinic (BC) conversion rates defined, e.g. [*Small et al.*, 2009], 443 by

444

$$
BT = -\rho_0 \left\langle u' \bullet \left( u' \bullet \frac{\partial U}{\partial x}, u' \bullet \frac{\partial U}{\partial y} \right) \right\rangle
$$

$$
BC = -g \left\langle \rho' w' \right\rangle
$$

445 where angle bracket denotes a depth average, *u*' and *U* are the depth dependent ocean 446 eddy and large scale current, respectively. Fig. 15c shows the depth average and 447 longitude average of the BT and BC for the CTL. The BT has a peak near the equator due 448 to the meridional shear between the EUC and north branch of the South Equatorial 449 Current, while the BC has a peak at around 3<sup>°</sup>N due both to temperature gradient and 450 vertical shear of the equatorial currents [*Small et al.*, 2009]. The BT and BC are reduced 451 in the DEP20\_LEV05 (Fig. 15d). This result reveals that the EKE associated with the

452 TIW is weakened due both to the reduction of the meridional and vertical shear of the 453 equatorial currents and temperature gradient.

## 454 **4. Summary and Discussion**

455 Small Vertical Scale structures (SVSs) have been observed to contribute greatly to 456 vertical mixing in and above the equatorial thermocline. Their scale is such that they are 457 typically unresolved by OGCMs. We have investigated the role of the elevated vertical 458 mixing induced by the SVSs in the thermocline in the equatorial Pacific. It has been 459 found that the elevated background vertical mixing affects the state of equatorial Pacific. 460 We have found that the enhanced mixing sharpens the thermocline and reduces the 461 stratification above the thermocline through the Phillips effect [*Phillips*, 1973]. The 462 sharpened thermocline limits the exchange of heat across the thermocline and tends to 463 trap heat above the thermocline in the eastern equatorial Pacific. The reduced 464 stratification allows the mixed layer to deepen more during times of entrainment but leads 465 to less cooling of the mixed layer and hence SST. The amplitude of the annual cycle in 466 SST is reduced and the annual mean SST increased when compared to the case with no 467 SVS enhanced mixing. These changes are in stark contrast to those obtained when the 468 background vertical diffusivity coefficient is enhanced throughout the depth of the water 469 column, which leads to a more diffuse thermocline, greater cooling during entrainment 470 and a colder annual mean SST

471 SVS-induced mixing also reduces the stratification, and sharpens and deepens the 472 thermocline in the western equatorial Pacific. The thermocline in the western equatorial 473 Pacific, however, is much deeper than that in the eastern equatorial Pacific. The enhanced 474 vertical mixing in the western equatorial Pacific brings up relatively cooler waters to 475 reduce the temperature in the upper ocean.

476 It has been found that the mixing induced by SVSs reduces the amplitude of the 477 annual cycle of both the mean and eddy advective heat fluxes, while producing virtually 478 no change to the total advective heat flux. The mixing induced by SVSs reduces the EKE 479 associated with the TIWs through a reduction of the meridional and vertical shear of the 480 equatorial currents and temperature gradient.

481 Our work demonstrates the importance of the vertical distribution of the vertical 482 mixing by unresolved processes (the background vertical diffusivity). We have chosen to 483 use a particularly simple parameterization to show the role of mixing induced by SVSs. A 484 more physically based parameterization scheme for the mixing induced by SVSs will 485 need to take the generation mechanism into account. *Richards et al.* [2011] speculate that 486 the observed SVSs are caused by a combination of instabilities of the flow and wind 487 generated inertia-gravity waves. The SVS induced mixing will therefore be temporally 488 and spatially variable. Indeed, *Richards et al.* [2011] find large differences in the vertical 489 diffusivity in the western equatorial Pacific between El Niño and La Niña states, brought 490 about principally by changes to the stratification between the bottom of the mixed layer 491 and the main thermocline. This leads us to speculate on the possibility of feedbacks in the 492 coupled system. A warmer cold tongue reduces the east-west pressure gradient in the 493 atmosphere, which in turn reduces upwelling in the ocean further warming the cold 494 tongue (the Bjerknes feedback, *Bjerknes* 1969; see also *Richards et al.* 2009). Initial 495 experiments with a coupled model show the warming of the cold tongue when SVS 496 mixing is added to be increased, as expected (results to be reported elsewhere). The



497 vertical mixing induced by SVSs may thus reduce the strong cold SST bias in the eastern

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#### 592 **Table captions**

593 Table 1. List of experiments. "DEP" denotes the isotherm to be which SVS mixing is

- 594 applied (°C). "LEV" denotes the magnitude of the SVS mixing  $(m^2s^{-1})$ . Details are
- 595 described in the right column. Background vertical diffusivity coefficients associated
- 596 with SVS mixing are computed at every time step. The background vertical diffusivity
- 597 coefficients in the equatorial Pacific and those outside of the region are linearly
- 598 interpolated (c.f. Fig. 1).
- 599
- 600 Table 2. The 20°C isotherm depth  $(D_{20})$  and thickness of thermocline  $(\Delta D_{16-22})$ . The
- 601 thickness of the thermocline is defined as the distance between isotherms of 16˚C and 602 22˚C. Unit is meter.
- 603

604 Table 3. Position of the core of the EUC, designated as the vertical grid point in which 605 the annual mean of the zonal velocity averaged between 1˚S-1˚N has the maximum. Bold 606 shows that the position of the core of the EUC of the run is deeper than that of CTL. Unit 607 is meter.

608

#### 610 **Figure captions**

611 FIG. 1 Background vertical diffusivity coefficients at 0˚N, 160˚E for (a) DEP20\_LEV05

- 612 and (b) DEP15\_LEV05. Unit is  $m^2s^{-1}$ .
- 613
- 614 Fig. 2 (a) The annual mean of SST in CTL. (b) The annual mean of temperature averaged
- 615 over the latitudinal band 2˚S-2˚N simulated by the OGCM (black) and observed (red).
- 616 The 16, 20, and 22˚C isotherms are shown for the observed temperature. (c) The annual
- 617 cycle of SST averaged over the latitudinal band 2˚S-2˚N. (d) Observed annual mean of
- 618 zonal current averaged over the latitudinal band 1˚S-1˚N. (e) As in (d), but for the zonal
- 619 current simulated in CTL. Unit is  $^{\circ}$ C for (a-d) and ms<sup>-1</sup> for (d and e).
- 620

621 FIG.3 (a) The annual mean of SST averaged over the latitudinal band 2˚S-2˚N. (b) The

622 annual cycle of SST at 0˚N, 170˚E (solid) and 0˚N, 120˚W (dotted). Black and red shows

- 623 the observation and model result, respectively. Unit is ˚C.
- 624

625 FIG. 4 A difference in the annual mean of SST between simulations with and without

626 SVS mixing (with minus without SVS mixing). Unit is ˚C. The contour interval is 0.5˚C.

627

628 Fig. 5 (a-c) A difference in the annual mean of temperature along the equator between

629 simulations with and without SVS mixing (with minus without SVS mixing). The

- 630 contour shows the isotherm line of 16, 20, and  $22^{\circ}$ C. Unit is  $^{\circ}$ C. (d-f) The annual mean of
- 631 zonal current along the equator (contour) and a difference in the annual mean of the zonal
- 632 current between simulations with and without SVS mixing (color). Unit is ms<sup>-1</sup>

635  $2^\circ$ S-2°N. The unit is  $^\circ$ C. 636 637 FIG. 7 The annual cycle of the tendency terms for the mixed layer heat budget averaged 638 over the region 2˚S-2˚N, 140˚W-90˚W in (a) CTL, (b) DEP20\_LEV05, (c) DEP0\_LEV05, 639 and (d) DEP20\_LEV1. Red shows the atmospheric forcing term. Blue shows the sum of 640 the entrainment and diffusive flux at the mixed layer base. Cyan and purple denote the 641 lateral diffusion and advection, respectively. Black shows the temperature tendency. The 642 unit is  $^{\circ}$ C day<sup>-1</sup>. 643 644 Fig. 8 The tendency terms for the mixed layer heat budget averaged over the region 2˚S-645 2˚N, 140˚W-90˚W for the July-February mean in CTL (white), DEP0\_LEV05 (green), 646 DEP20\_LEV05 (red), and DEP20\_LEV1 (blue). The left, central, and right part show the 647 atmospheric forcing, advection, and vertical diffusion term, respectively. Unit is  ${}^{\circ}C$  day<sup>-1</sup>. 648 649 FIG. 9 As in Fig. 7, but for the March-June mean. 650 651 Fig. 10 (a) The annual cycle of the square of the buoyancy frequency  $(x10^{-4} s^{-2})$ , contour) 652 averaged over the region 2˚S-2˚N, 120˚W-100˚W in CTL. (b-d) Difference in the vertical 653 diffusivity coefficient  $(x10^{-4} \text{ m}^2 \text{s}^{-1})$ , color shaded) and the square of the buoyancy 654 frequency  $(x10^{-4} s^2)$ , contour) between simulations with and without SVS mixing,

634 FIG. 6 As in Fig. 4, but for the annual cycle of SST averaged over the latitudinal band



655 respectively. Contours in cyan and green denote the annual cycle of the mixed layer depth

678 for CTL. Blue and green denote the mean and eddy advection terms for DEP20\_LEV05.

679 Table 1. List of experiments. "DEP" denotes the isotherm to be which SVS mixing is 680 applied (°C). "LEV" denotes the magnitude of the SVS mixing  $(m^2s^{-1})$ . Details are 681 described in the right column. Background vertical diffusivity coefficients associated 682 with SVS mixing are computed at every time step. The background vertical diffusivity 683 coefficients in the equatorial Pacific and those outside of the region are linearly 684 interpolated (c.f. Fig. 1).



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698 and (b) DEP15\_LEV05. Unit is  $m^2s^{-1}$ .



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707 Fig. 3 (a) The annual mean of SST averaged over the latitudinal band 2˚S-2˚N. (b) The 708 annual cycle of SST at 0˚N, 170˚E (solid) and 0˚N, 120˚W (dotted). Black and red shows 709 the observation and model result, respectively. Unit is ˚C.



 $\begin{array}{c} 711 \\ 712 \end{array}$ Fig. 4 A difference in the annual mean of SST between simulations with and without

713 SVS mixing (with minus without SVS mixing). Unit is ˚C. The contour interval is 0.5˚C.



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715 Fig. 5 (a-c) A difference in the annual mean of temperature along the equator between 716 simulations with and without SVS mixing (with minus without SVS mixing). The 717 contour shows the isotherm line of 16, 20, and 22°C. Unit is °C. (d-f) The annual mean of 718 zonal current along the equator (contour) and a difference in the annual mean of the zonal 719 current between simulations with and without SVS mixing (color). Unit is ms<sup>-1</sup>.



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<sup>722 2°</sup>S-2°N. The unit is °C.



723

724 Fig. 7 The annual cycle of the tendency terms for the mixed layer heat budget averaged 725 over the region 2˚S-2˚N, 140˚W-90˚W in (a) CTL, (b) DEP20\_LEV05, (c) DEP0\_LEV05, 726 and (d) DEP20\_LEV1. Red shows the atmospheric forcing term. Blue shows the sum of 727 the entrainment and diffusive flux at the mixed layer base. Cyan and purple denote the 728 lateral diffusion and advection, respectively. Black shows the temperature tendency. The 729 unit is  $^{\circ}$ C day<sup>-1</sup>.



731 Fig. 8 The tendency terms for the mixed layer heat budget averaged over the region 2˚S-

732 2˚N, 140˚W-90˚W for the July-February mean in CTL (white), DEP0\_LEV05 (green),

733 DEP20\_LEV05 (red), and DEP20\_LEV1 (blue). The left, central, and right part show the

734 atmospheric forcing, advection, and vertical diffusion term, respectively. Unit is °C day<sup>-1</sup>.



736 Fig. 9 As in Fig. 7, but for the March-June mean.



737 Fig. 10 (a) The annual cycle of the square of the buoyancy frequency  $(x10^{-4} s^{-2})$ , contour) 739 averaged over the region 2˚S-2˚N, 120˚W-100˚W in CTL. (b-d) Difference in the vertical 740 diffusivity coefficient  $(x10^{-4} \text{ m}^2 \text{s}^{-1})$ , color shaded) and the square of the buoyancy 741 frequency  $(x10^{-4} s^2)$ , contour) between simulations with and without SVS mixing, 742 respectively. Contours in cyan and green denote the annual cycle of the mixed layer depth 743 and 20°C isotherm, respectively. 744



746 Fig. 11 (a) Vertical distribution of the annual mean of background vertical diffusivity 748 coefficient averaged over the region 2˚S-2˚N, 120˚W-100˚W for DEP20\_LEV05 (black), 749 DEP15\_LEV05 (red), and DEP15\_LEVvar (green). The decimal logarithm is taken for 750 the background vertical diffusivity coefficient. Vertical axis shows the water depth (m). 751 Unit is  $m^2s^{-1}$ .



753 Fig. 12 As in Fig. 7, but for the western equatorial Pacific (2˚S-2˚N, 160˚E-140˚W).



756 Fig. 13 As in Fig. 8, but for the annual mean for the western equatorial Pacific.



759 Fig. 14 As in Fig. 10, but for the western equatorial Pacific (2˚S-2˚N, 160˚E-140˚W). 



761 Fig. 15 The annual mean of the eddy kinetic energy averaged from the surface to 100m 763 depth for (a) CTL and (b) DEP20\_LEV05. Unit is Jm<sup>-3</sup>. (c) Red and blue lines show the 764 barotropic and baroclinic conversion terms for CTL, respectively. Unit is  $10^{-5}$  kg/ms<sup>3</sup>. (d) 765 As in (c) but for the DEP20\_LEV05.



767<br>768 Fig. 16 The annual cycle of the mean and eddy advection terms averaged over the

769 region140˚W-90˚W, 2˚S-2˚N. Red and orange denote the mean and eddy advection terms

770 for CTL. Blue and green denote the mean and eddy advection terms for DEP20\_LEV05.